

Distinct Element Modeling of Masonry-Infilled Steel Frames with Openings

Amin Mohebkhah^{*1} and A.A. Tasnimi²

¹Struct. Eng. Dept., Faculty of Civil and Architectural Eng., Malayer University, Malayer, Iran; ²Structural Eng. Div., Faculty of Civil & Env. Eng., Tarbiat Modares University, Tehran, Iran

Abstract: Numerical analysis of masonry-infilled steel frames (MISFs) is one of the greatest challenges faced by structural engineers. This difficulty results from the presence of joints as the source of discontinuities and nonlinearities as well as the interaction of frame-infill panel. In spite of many studies performed on numerical modeling of solid MISFs, there are few studies on MISFs with openings. A 2D numerical model using the specialized distinct element software UDEC (2004) for the pushover analysis of MISFs with openings is developed. In this model, large displacements and rotations between masonry bricks are taken into account. A comparison between the results of distinct element modeling and the experimental results available in the literature showed a good correlation between them. Furthermore, It was found that the model has the capability to predict lateral load capacity, joint cracking patterns and explore the possible failure modes of MISFs with openings.

Keywords: Masonry-infilled steel frame, distinct element method, opening, pushover analysis, numerical modeling, micro-modeling.

1. INTRODUCTION

Steel framed buildings are usually infilled with masonry panels as partition and surrounding walls. The composite steel-masonry framed building is called masonry-infilled steel frame (MISF) which has high lateral stiffness and load capacity. Under severe lateral forces, the surrounding frame interacts with the infill masonry panel increasing lateral stiffness and load capacity of the MISF. This is because, the frame and masonry infill panel deform in a bending and shear modes, respectively. In spite of the frame-infill panel interaction, the unexpected effects of infill panels are not usually taken into account in the analysis and design of such frames. Ignoring the structural effects of infill panels may results in wrong estimation of lateral stiffness, capacity and ductility of these frames.

Since 1950's, many numerical and experimental researches have been conducted on the behavior of MISFs. Stafford Smith [1, 2], Riddington and Stafford Smith [3], Liauw and Kwan [4] and Moghadam *et al.* [5] have performed numerical and experimental studies on the lateral stiffness and load capacity of MISFs. Extensive findings of the previous studies conducted until 1987 have been presented in the state-of-the-art report on MIFs by Moghadam and Dowling [6].

Numerical modeling strategies of infilled frames are divided into two distinct categories, *micro-modeling* and *macro-modeling*. For micro-modeling of masonry-infilled frames, both the surrounding frame and the infill panel components details are established using a numerical method

such as finite element method (FEM) or distinct/discrete element method (DEM). In this method, the interaction between masonry bricks along the joints as well as the frame-infill panel interaction is taken into account. In the literature, Mehrabi and Shing [7] have proposed a smeared-crack nonlinear finite element model to study the nonlinear behavior of infilled reinforced concrete frames. Dawe and Seah [8] developed an innovative model for analyzing the interaction of frames with infill panels which includes the effects of variables such as design gapping between panel and frame, and rigid connectivity between panel and frame. Asteris [9] using a new finite element technique, investigated the influence of the masonry infill panel opening in the reduction of the infilled frames stiffness. It was found that the overall action between the frame and the infill is adversely affected as the opening position is moved towards the compression diagonal [9].

Despite the abovementioned numerical studies, it seems that the lateral load behavior of MISFs cannot be properly investigated by continuum mechanics based methods such as traditional finite element method. However, some advanced finite element programs such as DIANA (developed in Ref. [10]), include interface elements that allow the user to incorporate masonry discontinuities in the analysis properly and correctly. As an alternative to the available finite element methods, a distinct/discrete element method (DEM) can be used to investigate the nonlinear lateral load behavior of MISFs. Distinct element method has the capability to consider large displacements, shear sliding and complete joints openings between bricks as well as automatic detection of new contacts during the analysis process [11]. Mohebkhah *et al.* [12] developed a 2D distinct/discrete element model for the inelastic analysis of concrete masonry-infilled steel frames which considers both geometric and material nonlinearities.

*Address correspondence to this author at the Struct. Eng. Dept., Faculty of Civil and Architectural Eng., Malayer University, Malayer, Iran; Tel: +98 0851 2232346; Fax: +98 0851 2221977; E-mail: amoheb@malayeru.ac.ir

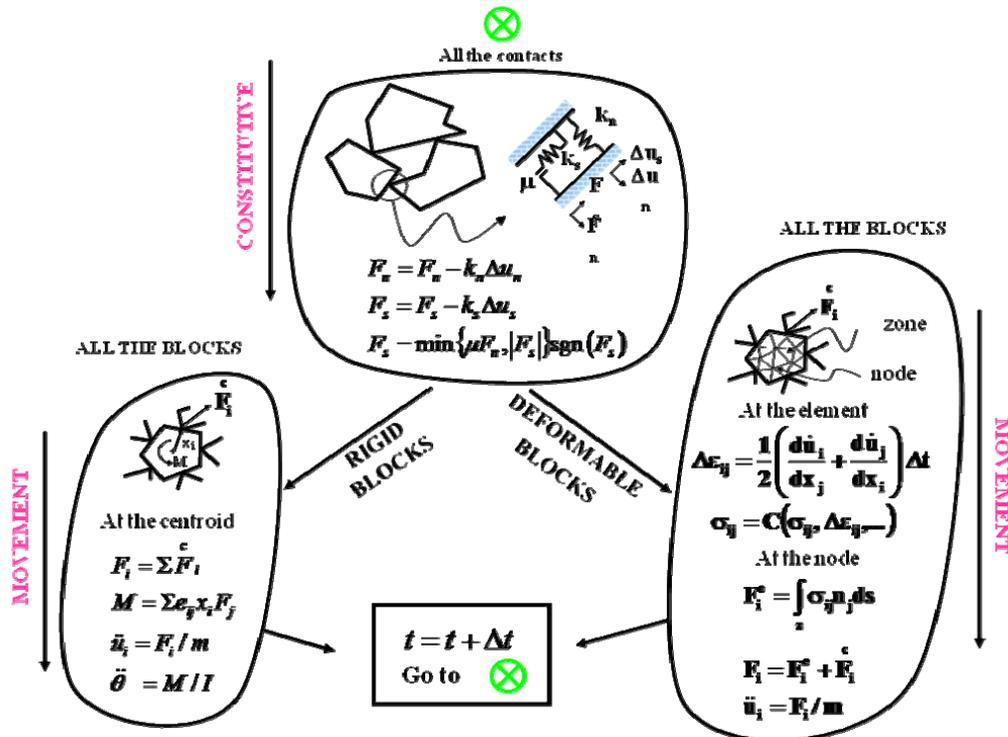


Fig. (1). Calculation cycle for the distinct element method [11]

The purpose of this paper is to simulate the nonlinear lateral load behavior of clay brick masonry-infilled steel frames with openings. To achieve this end, the 2D distinct element model developed previously in Ref. [12] using the specialized distinct element software UDEC (2004) [11], is developed and presented in more detail in this paper for the push-over analysis of MISFs with openings.

2. DISTINCT ELEMENT METHOD

Distinct/discrete element methods (DEMs) were initially developed for the study of jointed and fractured rock masses in 1971 by Prof. P. Cundall as reported in [13]. Owing to their ability to take into account the relative motion of jointed blocks, these methods are useful for the analysis of masonry structures in which a significant part of the deformation is due to relative motion between the bricks. There are different applications of DEMs for static or dynamic analysis of masonry structures in the literature [14-17]. All the models in this paper were analyzed using the specialized distinct element software UDEC (Itasca, 2004). The Universal Distinct Element Code (UDEC) is a 2D program based on the DEM to simulate the behavior of jointed materials subjected to either static or dynamic loading. In the program, the jointed material is modeled as an assemblage of distinct blocks and the joints are considered as boundary conditions between blocks. Furthermore, large displacements along joints and rotations of blocks are permitted [11]. Distinct blocks can be modeled as either rigid or deformable material. Deformable blocks are subdivided into a mesh of finite-difference triangular elements, and each element behaves according to a defined linear or nonlinear stress-strain law [11]. The formulation of these elements is similar to the constant strain triangle (CST) finite element formulation. The drawback of this element is that, for complicated continuum

problems such as beam/column components behavior in a MISF, a very large number of triangular elements has to be used to discretize the component. To model the contact between blocks, it is presumed that the blocks are jointed by normal and shear elastic springs [11]. The relative motion of the joints is also prescribed by linear or nonlinear force-displacement relations for movement in both the normal and tangential directions.

The original UDEC program developed by Cundall was based on the plane strain situation [11]. In the UDEC 4.0 version, the plane stress situation which is encountered in masonry walls subjected to in-plane loading can be also described. The computations performed in the DEM alternate between the application of a force-displacement law at all interfaces and Newton's second law at all blocks or nodes [11]. The force-displacement law is used to find interface forces between blocks from known displacements. Newton's second law gives the motion of the blocks resulting from the known forces acting on them. Fig. (1) shows schematically the calculation cycle for the distinct element method [11]. Mechanical damping is used in the DEM to solve both static and dynamic solutions. For each class, a different type of damping is used. For static analysis, an approach similar to dynamic relaxation technique is employed [11]. In this technique, the equations of motion are damped to reach the equilibrium state as soon as possible.

3. DEM MODELING OF MASONRY-INFILLED STEEL FRAMES

The abovementioned distinct element method is utilized here to simulate the nonlinear lateral load behavior of some brick MISFs tested at the Building and Housing Research Center (BHRC) by Tasnimi and Mohebkhah [18]. In the test

Table 1. Properties of Test Specimens [18]

Specimen	Configuration	Prism strength (MPa)
BF	Bare frame	-----
SW	Solid infilled frame	7.4
PW1	Infilled frame with 500×500 mm window opening	7.4
PW2	Infilled frame with 700×800 mm window opening	7.0
PW3	Infilled frame with 1200×600 mm window opening	7.0
PW4	Infilled frame with 700×1450 mm door opening	8.5

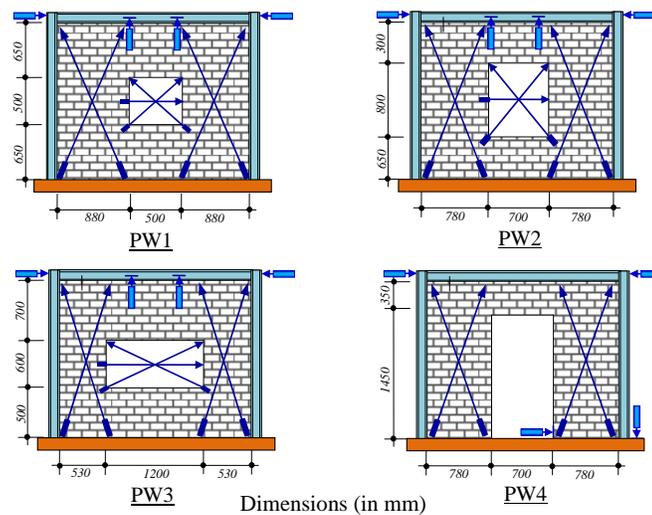


Fig. (2). Configuration and position of LVDTs and DPC electrical transducers of Test Specimens [18].

Table 2. Properties of Masonry Infills and their Constituents [19]

Characteristics	Brick	Mortar	Brickwork		
			SW, PW1	PW2, PW3	PW4
Comp. strength (MPa)	12.6	10.1	7.4	7.0	8.5
Tensile strength (MPa)	0.48	0.5	0.12	0.12	0.12
Young's Modulus (MPa)	8442	1000	5194	4900	5985
Cohesion (MPa)	3.64	0.48			
Internal friction angle (degree)	30	36			

program, six large-scale single-story single-bay steel frames were constructed and tested under cyclic quasi-static lateral in-plane loading. All specimens were 2400 mm long by 1870 mm high. Infill panels consisted of 219 × 110 × 66 mm solid clay bricks (with no voids) placed in running bond with 22 courses within a surrounding moment-resistant steel frame fabricated using IPE140 sections ($A = 16.4 \text{ cm}^2$, $I_{xx} = 541 \text{ cm}^4$, $d = 14$, $bf = 7.3$, $tf = 0.69$, $tw = 0.47 \text{ cm}$). The single wythe infill panel thickness in all specimens was 110 mm. One frame was tested without an infill panel (bare frame), one had a solid infill panel, and the others had infill panels

with symmetrical window or door openings. Table 1 summarizes the properties of each specimen and Fig. (2) illustrates the geometry and dimensions of the test specimens. Lintel beams consisting of two L30×30×3 steel shapes were used to span openings and were extended on each side an additional 150 mm. IPE140 steel sections had a yield stress of 315 MPa. Complete description of the specimens can be found in Ref. [18]. The mechanical properties of masonry panels and their constituents required for the DEM analyses are as shown in Table 2 [19].

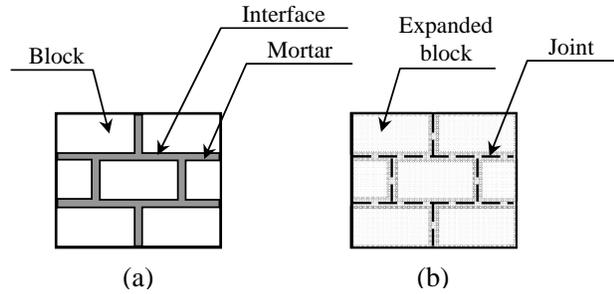


Fig. (3). Micro-modeling strategies for masonry walls: (a) detailed; and (b) semi-detailed.

The specimens were modeled at a semi-detailed level using DEM. At a semi-detailed level, the joint is modeled as a zero thickness interface element, in analogy with the discontinuum finite element modeling [10]. In this approach, instead of detailed modeling of masonry constituents (i.e. both bricks and mortar) as shown in Fig. 3(a), brick dimensions are expanded virtually in which each dimension is of the same size as the original dimension plus the real joint thickness as shown in Fig. 3(b). The interface's stiffness is calculated from the stiffness of the real joint. The behavior of bricks is assumed to be described by an inelastic isotropic model. The bricks are considered fully deformable, thus allowing deformation to occur both in the bricks and joints. To determine the specimens collapse loads, a displacement-controlled boundary condition is adopted. Hence, an incremental horizontal displacement was applied at the top left corner of the models.

3.1. Elastic Parameters

In order to develop a DEM micro-model based on interface elements with zero thickness, the size of the bricks has to be expanded by the mortar thickness h_m in both directions. It follows that the elastic properties of the *expanded brick* and the *interface joint* must be adjusted to produce accurate results. Because of the relative dimensions of mortar and brick, the elastic properties of the expanded brick are assumed to be the same as that of the real brick. Thus, the normal and shear joint stiffness values are estimated as follows [20]:

$$k_n = \frac{E_b E_m}{h_m (E_b - E_m)} \quad (1)$$

$$k_s = \frac{G_b G_m}{h_m (G_b - G_m)} \quad (2)$$

Where E_b and E_m are the Young's modulus, G_b and G_m are the shear modulus, respectively, for brick and mortar and h_m is the actual thickness of the mortar. The accuracy of this approach has been validated by Lourenco [10] using some detailed discontinuum finite element analyses.

3.2. Inelastic Parameters and Constitutive Criteria

Different parameters may affect the behavior and accuracy of the generated model. The constitutive model adopted to describe the material behavior is the most essential pa-

rameter in such analyses. UDEC version 4.0 has some built-in constitutive material models such as: isotropic elastic, Drucker-Prager, Mohr-Coulomb, strain-hardening/softening and etc. For the problem with low stress intensities, a linear-elastic constitutive material model is adequate. However, for high stress intensities a nonlinear constitutive material model which can take into account nonlinear phenomena such as crack formation and crushing is required. The nonlinear post-peak behavior of stone-like materials such as masonry is characterized by softening which determines the way in which crack formation propagates within a brick [20]. It has been observed that as the shear displacement increases, the brick cohesion gradually decreases to zero [10]. Therefore, the clay bricks behavior were described using a strain-hardening/softening material model. This model is based on the UDEC Mohr-Coulomb model with tension cut-off in conjunction with non-associated shear and associated tension flow rules. Softening model for bricks is described using softening rate of tensile strength and cohesion of bricks as follows [20]:

$$\sigma = f_t e^{-\frac{f_t}{G_f^I} u} \quad (3)$$

$$c = c_u e^{-\frac{c_u}{G_f^{II}} v_p} \quad (4)$$

In which G_f^I denotes the tensile fracture energy (generally named Mode-I fracture energy) and is defined as the amount of energy to create a unitary area of a tension crack. Similarly, G_f^{II} stands for the shear fracture energy (generally named Mode-II fracture energy) and is defined as the amount of energy to create a unitary area of a shear crack. According to Ref. [10], parameter G_f^I for clay bricks ranges from 0.005 to 0.02 $N.mm/mm^2$ for a tensile strength ranging from 0.3 to 0.9 MPa and parameter G_f^{II} ranges from 0.01 to 0.25 $N.mm/mm^2$ for a cohesion strength ranging from 0.1 to 1.8 MPa . In this research the values of G_f^I and G_f^{II} were computed as 0.008 and 0.1 $N.mm/mm^2$ based on the relevant brick tensile and cohesion strengths.

Since the steel frame components in the model were expected to behave inelastically at high load levels, a Von-Mises material model was selected to characterize the steel frame behavior. The Von-Mises criterion is not available in UDEC. However, the Drucker-Prager criterion can be degenerated into the Von-Mises criterion for $\varphi=0$ [11]. The steel frame members (i.e. the steel beam and columns I-sections) were replaced with their equivalent solid rectangular blocks of steel having the same elastic and inelastic mechanical properties.

For the mortar joints, a Mohr-Coulomb slip model is used. The average angle of internal friction and cohesion of the mortar joints (φ_j , c_j) are 36° and 0.48 MPa , respectively [19]. The other essential inelastic parameter is the dilation angle. Dilatancy refers to an expansion in masonry volume that takes place when shear stress is applied to a material. This expansion is demonstrated by a dilation angle, ψ_j , which measures the uplift due to shearing. It has been shown [21, 22] that dilatancy must be considered in the analysis of confined masonry structures such as infilled frames. The dilatancy angle ψ_j depends on the level of the applied confin-

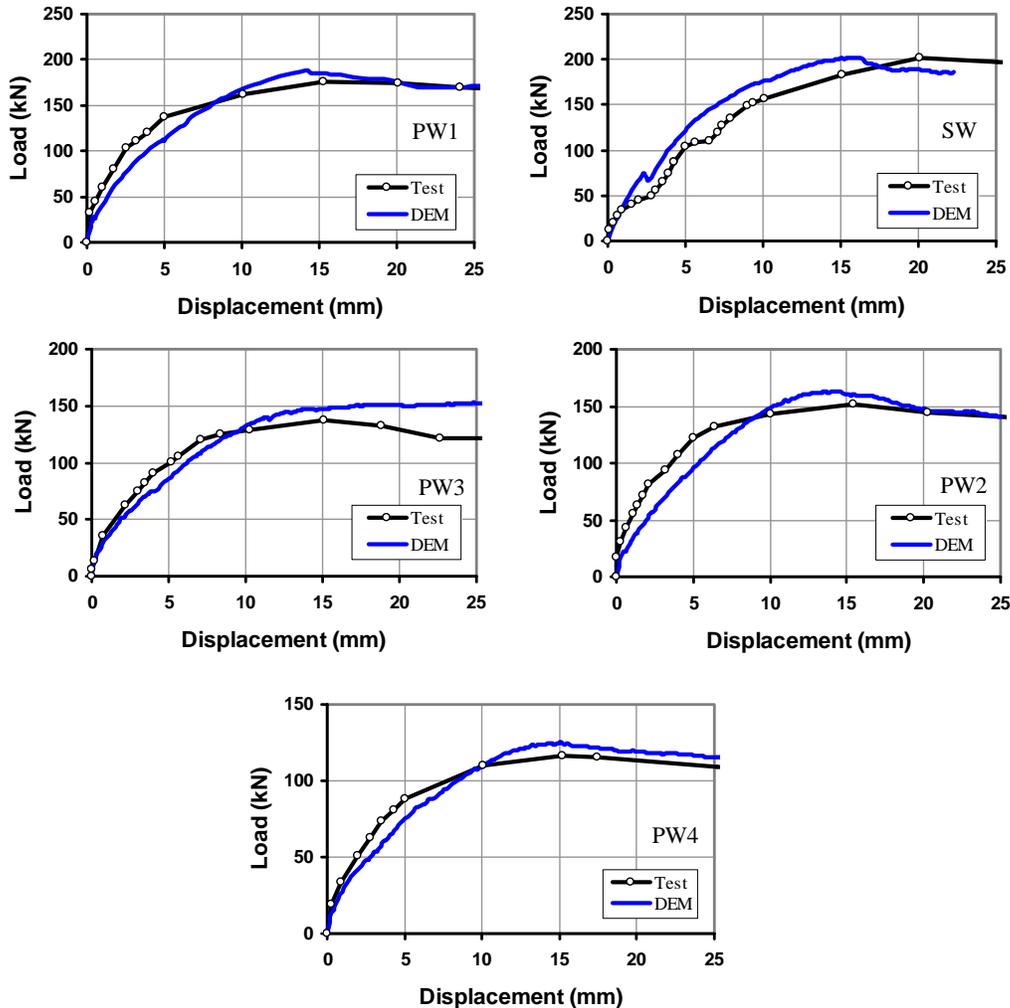


Fig. (4). Lateral load–displacement diagrams for all the analyzed specimens.

ing stress; as for high confining pressures (e.g. masonry infill panels) the average value of $\tan\psi_j$ is about 0.2 [10]. Therefore, in this paper, tangent of the dilatancy angle of 0.2 (approximately $\psi_j = 12^\circ$) was chosen for the joints.

The other essential parameter that must be chosen is the friction between steel members and masonry infill wall. Therefore, a coefficient of friction equal to 0.25 was assumed for the frame-to-infill wall interfaces [8].

4. ANALYSIS AND COMPARISON WITH TEST RESULTS

The 2D distinct element model generated in this study was employed to simulate the behavior of brick masonry-infilled steel frame specimens described in section 3. Fig. (4) illustrates the comparison between the load-displacement relationships of all the experimented specimens, and that of the DEM analysis, up to failure mechanism formation. The local peaks in the curves are attributed to the state at which a new joint cracking occurs or plastic failure takes place in the bricks. Also, Table 3 presents the difference between the numerical and experimental ultimate collapse loads. As it

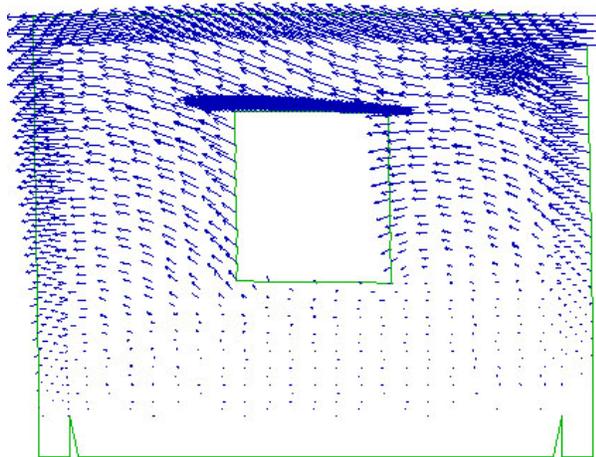
can be seen, the experimental and numerical results comparison shows a good correlation between them. The maximum error of the numerical analysis is 13% for specimen PW3 and an average error of 5% for the other four specimens. The relative large difference in the load capacity value of specimen PW3 can be attributed to premature failure of slender side piers in the test. In other words, the weak bricks may have induced a premature diagonal shear cracking failure of the slender piers leading to a low capacity.

Together with the global load-displacement relationships, a comparison in terms of the deformed geometry, displacement vectors and the failure mechanism is needed to investigate the accuracy of the DEM results. In Fig. (5), displacement vectors of specimen PW2 at the time of ultimate capacity (lateral displacement equal to 25 mm) are shown. As it is observed, lateral deformation of the infill panel takes place mainly in the side piers and the top masonry spandrel beam. The bottom masonry spandrel beam deformation is insignificant and can be ignored. Therefore, it can be concluded that ductility of the infilled frame depends on the failure mode of side infill piers (i.e. force-controlled or displacement-

Table 3. Comparison of Experimental and Numerical Collapse Loads

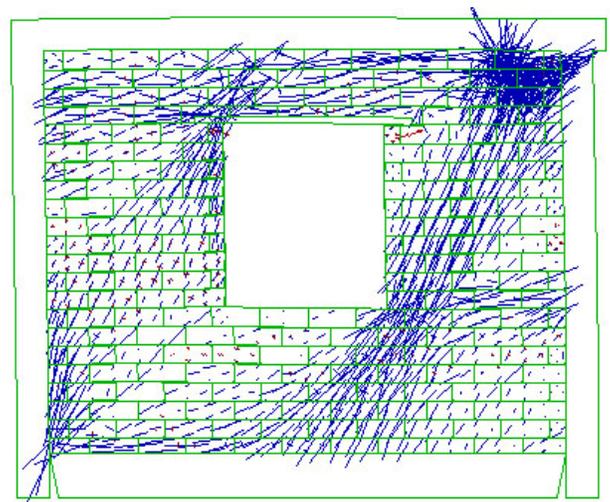
<i>Specimen</i>	<i>Experimental (kN)</i>	<i>Numerical (kN)</i>	<i>Ratio (Num./Exp.)</i>
SW	201.5	202	1.00
PW1	176.1	187	1.06
PW2	151.9	163	1.07
PW3	137	150	1.13
PW4	116.5	125	1.07

controlled failure modes). Also, it can be observed that the effective height of right pier is less than that of the left pier. In other words, the right pier is treated as a short pier and due to the confinement by the adjacent steel beam and column, it has the main role in lateral load capacity of the infilled frame. As it is seen in Fig. (5), for DEM modeling of steel frame, the columns' bottom has been extended downward. This has been done deliberately on the contrary to the test specimen. Because, it is not possible to fix the columns' bottom in UDEC program manually; just translational displacements can be restrained in each node. Hence, the columns elongated downward additionally while restraining all the surrounding nodes, to simulate fixed boundary conditions provided in the test program. The bottom two triangles have been deleted from the whole model for this reason (restraining the surrounding nodes of the column bottom). Moreover, the strong floor under the infill panel has been modeled as an elastic steel beam.

**Fig. (5).** Displacement vectors for specimen PW2.

The principal stresses tensor for the PW2 model at ultimate capacity is shown in Fig. (6). In this figure, principal stresses directions show the orientation of the activated compressive parts orientation of the infill wall under lateral loading. Because of the presence of opening, the infill wall is forced to act as four distinct parts including one horizontal (top spandrel) and three inclined (side piers and bottom spandrel) compressive struts. The horizontal strut connects the windward column top to the two inclined compressive struts to resist the applied lateral load.

The state of inelastic bricks is represented using some plastic indicators in UDEC program. These indicators denote that plastic flow is occurring, but it is possible for a brick mesh element simply to sit on the yield surface without any significant flow taking place. The collapsed joints as well as the plastic behavior in the bricks are shown in Fig. (7). The failure situation of the elements is shown in this figure using three distinct symbols: \times , $*$ and \circ indicating “yielding in past”, “at yield surface” and “tensile failure”, respectively. The situation “yielding in past” shows the unloaded yielding elements so that their stresses no longer satisfy the Mohr-Coulomb yield criterion [11]. As well, the situation “at yield surface” demonstrates the actively yielding elements which are important to the detection of a failure mechanism. The pattern of cracking and failure points as predicted by the numerical analysis is in good agreement with the experimental observations given in [18]. Also, as shown in Fig. (7), the surrounding frame elements yield in two points (on top beam and windward column) where the activated inclined compressive struts interact with them. This indicates the importance of short column effect that must be considered in column design of such frames, especially in masonry infilled reinforced concrete frames. The experimentally obtained cracking and failure pattern of the specimen at a lateral displacement of 25 mm is shown in left part of Fig. (7). It is evident that the pattern of infill panel cracking and diagonal tension failure (in side piers and bottom spandrel beam) as

**Fig. (6).** Magnified principal stress tensors for specimen PW2 infill panel.

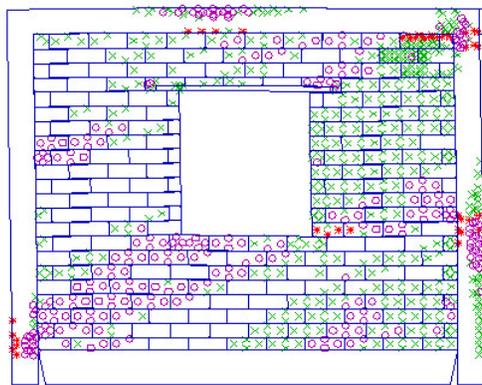


Fig. (7). Elements' failure points and crack patterns of the joints for specimen PW2 (numerical and experimental [19] results).

predicted by the DEM is compatible with laboratory experimental findings. The diagonal tension failure points have been distinguished from the others by the symbol \circ . As it can be seen in the test failure pattern in Fig. (7), masonry side piers undergo sudden diagonal brittle failures (localized fracture through bricks) which cannot be properly captured by finite element-based plasticity models such as Mohr-coulomb failure criterion. That's why the extent of DEM failure seems slightly different compared to the test. These kinds of failures can be simulated properly using fracture mechanics principles. As an alternative, the failure can be simulated in future DEM studies using the potential brick cracks as proposed by Lourenco in his PhD dissertation [10].

6. CONCLUSION

A 2D distinct element model developed for the inelastic nonlinear analysis of masonry-infilled steel frames. A micro-modeling approach was used to model masonry infill wall in which the joint is modeled as a zero thickness interface element. The bricks and joints are assumed fully deformable to simulate bricks failure points and joints sliding.

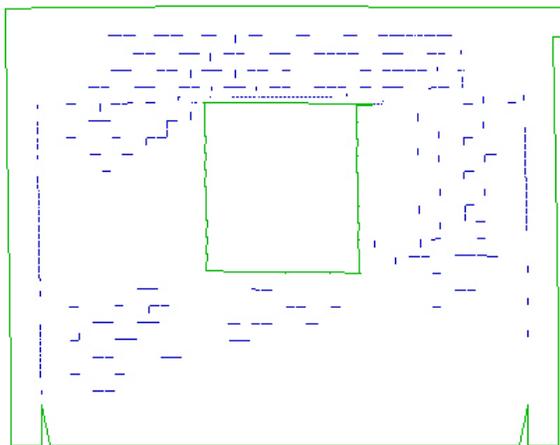


Fig. (8). Plot of joints with zero normal or shear stresses (joint sliding).

Figs. (8) and (9) show the plot of joint sliding and joint openings in the infill panel, respectively. As can be seen, the nonlinear behavior comes from the bricks than the joints.

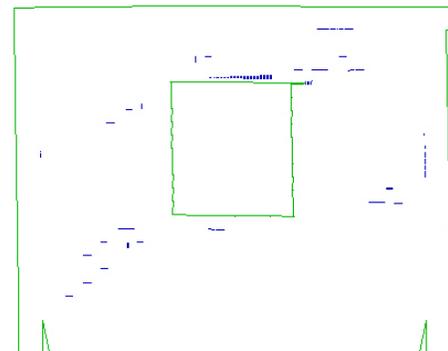


Fig. (9). Plot of joint opening.

Fig. (10) shows the magnified picture of the deformed geometry of specimen PW2. The separations and geometry distortions of the bricks (indicating cracking and crushing of the bricks) is clearly observed in the figure. Therefore, the obtained results reveal the capacity of the DEM to model masonry infill walls behavior.

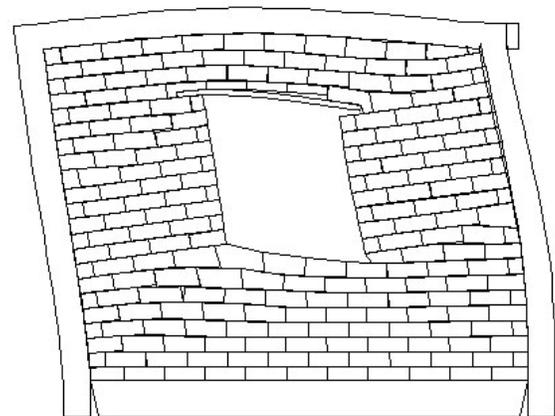


Fig. (10). Magnified deformed geometry for specimen PW2 (magnification factor = 10).

The developed model was used herein to simulate the lateral load behavior of some tested masonry-infilled steel

frames with openings reported in the literature. It was found that the DEM model is applicable to a detailed simulation of the nonlinear behavior of such frames throughout the loading process leading to failure. The prediction of lateral load capacity and the evolution of the deformations were both in agreement with the experiments. It was shown that the method can simulate confidently the failure mechanisms based on joint separation and sliding.

NOMENCLATURE

E_b	=	Young's modulus of brick masonry
E_m	=	Young's modulus of mortar
G_b	=	Shear modulus of brick masonry
G_m	=	Shear modulus of mortar
F_y	=	Yield stress of steel material
h_m	=	Thickness of the mortar
k_n	=	Normal joint stiffness ($N/mm^2/mm$)
k_s	=	Shear joint stiffness ($N/mm^2/mm$)
c	=	Brick masonry cohesion strength
ϕ	=	Brick masonry angle of internal friction
f'_c	=	Brick masonry compressive strength
c_j	=	Mortar joints cohesion strength
ϕ_j	=	Mortar joints angle of internal friction
ψ_j	=	Mortar joints angle of dilatancy

CONFLICT OF INTEREST

The author confirm that this article content has no conflicts of interest.

ACKNOWLEDGEMENT

Declared none.

REFERENCES

- [1] B. Stafford-Smith, "Lateral stiffness of infilled frames", *J. Struct. Div. ASCE*, vol. 88, no. ST6, pp. 183-199, 1962.
- [2] B. Stafford-Smith, "Behavior of square infilled frames", *J. Struct. Div. ASCE*, vol. 92, no. ST1, pp. 381-403, 1966.
- [3] J.R. Riddington, and B. Stafford Smith, "Analysis of infilled frames subjected to racking with design recommendations", *Struct. Eng.*, vol. 55, no. 6, pp. 263-268, 1977.
- [4] T.C. Liauw, and K.H. Kwan, "Unified plastic analysis for infilled frames", *J. Struct. Eng.*, vol. 111, no. 7, pp. 1427-1448, 1985.
- [5] H.A. Moghaddam, M.G.H. Mohammadi, and M. Ghaemian, "Experimental and analytical investigation into crack strength determination of infilled steel frames", *J. Construct. Steel Res.*, vol. 62, no. 12, pp. 1341-1352, 2006.
- [6] H.A. Moghaddam, and P.J. Dowling, "The state-of-the-art in infilled frames", ESEE Res. Rep. No. 87-2, Imperial College of Science and Technology, Civil Engineering Department, London, England, 1987.
- [7] A.B. Mehrabi, and P.B. Shing, "Finite element modeling of masonry-infilled RC frames", *J. Struct. Eng.*, vol. 123, no. 5, pp. 604-613, 1997.
- [8] J.L. Dawe, C.K. Seah, and Y.A. Liu, "Computer model for predicting infilled frame behavior", *Can. J. Civ. Eng.*, vol. 28, pp. 133-148, 2001.
- [9] P.G. Asteris, "Lateral stiffness of brick masonry infilled plane frames", *J. Struct. Eng.*, vol. 129, no. 8, pp. 1071-1079, 2003.
- [10] P.B. Lourenco, "Computational strategies for masonry structures", Ph. D. Thesis, Delft University of Technology, Delft, The Netherlands, 1996.
- [11] Itasca Consulting Group, Inc. UDEC- Universal Distinct Element Code, version 4.0- User's manual, Minneapolis, MN, USA, 2004.
- [12] A. Mohebbkhan, A.A. Tasnimi, and H.A. Moghaddam, "Nonlinear analysis of masonry-infilled steel frames with openings using discrete element method", *J. Construct. Steel Res.*, vol. 64, no. 12, pp. 1463-1472, 2008.
- [13] V.M. Sharma, K.R. Saxena, and R.D. Wood, "Distinct Element Modeling in Geomechanics", Balkema: Rotterdam, 1999.
- [14] L.V. Lemos, "Discrete element modeling of the seismic behavior of stone masonry arches", Computer Methods in Structural Masonry-4, In Pande, Middleton and Kralj Eds., E and FN Spon: London, 1997, pp. 220-227.
- [15] G.E. Sincraian, and J.J. Azevedo, "Numerical simulation of the seismic behavior of stone and brick masonry structures", in *Proc. of the 11th European Conference on Earthquake Engineering*, Balkema, 1998.
- [16] G.E. Sincraian, J.V. Lemos, and C.S. Oliveira, "Assessment of the seismic behavior of stone masonry aqueduct using the discrete element method", in *Proc. 11th European Conference on Earthquake Engineering*, Balkema, 1998.
- [17] J.J. Azevedo, G.E. Sincraian, and J.V. Lemos, "Seismic behavior of blocky masonry structures", *Earthquake Spectra*, vol. 16, no. 2, pp. 337-365, 2000.
- [18] A.A. Tasnimi, and A. Mohebbkhan, "Investigation on the behavior of brick-infilled steel frames with openings, experimental and analytical approaches", *Eng. Struct.*, vol. 33, pp. 968-980, 2011.
- [19] A. Mohebbkhan, "A nonlinear-seismic model for brick-masonry-infill panels with openings in steel frames", Ph. D. Thesis, Tarbiat Modares University, Tehran, Tehran, Iran, Nov. 2007.
- [20] J.G. Rots, Ed, "Structural masonry: an experimental/numerical basis for practical design rules", Center for Civil Engineering Research and Codes (CUR), Balkema: Rotterdam, 1997.
- [21] R.H. Atkinson, B.P. Amadei, S. Saeb, and S. Sture, "Response of masonry bed joints in direct shear", *J. Struct. Eng.*, vol. 115, no. 9, pp. 2276-2296, 1989.
- [22] K.M. Mosalam, R.N. White, and P. Gergely, "Static response of infilled frames using quasi-static experimentation", *J. Struct. Eng.*, vol. 123, no. 11, pp. 1462-1469, 1997.

Received: November 30, 2011

Revised: March 16, 2012

Accepted: April 12, 2012

© Mohebbkhan and Tasnimi; Licensee Bentham Open.

This is an open access article licensed under the terms of the Creative Commons Attribution Non-Commercial License (<http://creativecommons.org/licenses/by-nc/3.0/>) which permits unrestricted, non-commercial use, distribution and reproduction in any medium, provided the work is properly cited.