Finite Element Method of Composite Steel-Concrete Beams Considering Interface Slip and Uplift

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Abstract:

Introduction:

In order to analyze the displacement and internal force of composite steel-concrete beams under the vertical load, The finite element solution of composite steel-concrete beams under concentrated loads considering the existence of interface slip and vertical uplift based on the basic idea of elastic mechanics was derived in this paper.

Method:

A new kind of stiffness equation of bar system was got and its correctness was demonstrated with experimental value, the problem of composite beams considering the existence of interface slip and vertical uplift was solved, avoiding to produce large amount of calculation with the body element method.

Results and Conclusion:

It can be seamlessly integrated into the current engineering design software, which provides effective help to practical engineering problems.

Keywords: Composite beam, Finite element, Interface slip, Vertical uplift, Element stiffness matrix, Composite steel, Concrete beams.

1. INTRODUCTION

Composite steel-concrete beam is a new type of structure. Shear connectors between steel girder and concrete slab make them work together as a whole to resist interface slip and vertical uplift at the interface [1]. This structure is widely used in our country’s urban overpasses and building structure because of its characteristics of light weight, large stiffness, good plasticity, high strength, good stability, good integrality, long durability and short construction period. In China, Nie [2 - 4] in Tsinghua University studied the ultimate bearing capacity of composite steel-concrete beams, the ultimate bending capacity and strength expression of composite beams considering the effect of interface slip are derived on the basis of experiment.

Yu [5] has studied the interface slip and deformation of composite steel-concrete beams under vertical load, the formula of slippage is given. On that basis, Liu [6] has derived the analytical solutions of composite steel-concrete beams under vertical load, which can be used to obtain analytical expressions of stress and displacement in each part of composite beams just one time.
Lin [7, 8] has studied the behavior of composite steel-concrete beams under a negative bending moment. Load-displacement relationships, crack formation and its developing process, slip distribution at the interface of steel girder and concrete slab, and the flexural strain results of shear connectors were measured and studied. And she has built a three-dimensional FE model for numerical simulation analysis on horizontally curved steel-concrete composite beams subjected to negative bending moment. Hou [9] has made dynamic analysis of simply-supported steel-concrete composite beams under moving loads, obtained the governing motion equations considering the interface slip between steel girder and concrete slab. In other countries, Salari [10] has studied the slip effect of composite steel-concrete beams and pointed out that finite element analysis of composite beams based on force unit is accurate, it is economic and practical. Barnard [11] obtained many results based on test research of the flexural behavior of composite steel-concrete beams. The results are as follows: The existence of relative slip at the interface of steel girder and concrete slab is mainly due to the deformation of the shear connector under the action of horizontal shear.

The vertical uplift at the interface is mainly caused by different bending stiffness of steel girder and concrete slab. The above two conclusions effectively proved that the bearing capacity of composite beams calculated by transformed section method is greater than the actual bearing capacity of beam. Fabrizio [12] obtained a beam finite element for the long-term analysis of steel-concrete composite decks taking into account the shear lag in the slab and the partial shear interaction at the slab-girder interface.

Andrea [13] has studied the non-linear analysis of composite steel–concrete beams using the displacement formulation of the finite elements technique and illustrated some aspects related to the convergence of the method by comparing solutions deriving from finite elements with 8, 10 and 16DOF. Ranzi [14] has derived a stiffness formulation for the analysis of composite steel–concrete beams with partial shear interaction based on the direct stiffness method. The above studies will provide important references to the design and calculation of composite steel-concrete beams, but they are all only considering the effect of interface slip on mechanical behavior of composite steel-concrete beams without considering the effect of vertical uplift.

The existence of the lift force between steel girder and concrete slab will reduce combination effect and stiffness of composite beams, and it will increase the deflection thus affect its bearing capacity. Therefore, it is necessary to conduct in-depth researches on the effect of interface slip and vertical uplift to the mechanical performance of composite beams. Fu [15] calculated the uplift between steel girder and concrete slab in theory, compared the calculation results with the test results and gave analytic solution of composite beams considering the interface slip and vertical uplift at the same time. But the result is complex and tedious.

It is difficult to be mastered by actual technical personnel. Static and dynamic calculation theories of functionally graded beams/plates are derived in literature [16 - 20], which solve the problems of deflection, stress and dynamic response. They consider also the transverse shear deformation effect without requiring shear correction factors, have great significance in engineering. However, the contact effects of multi-layer structures are not addressed in these theories.

In summary, the existence of interface slip is commonly considered but the vertical uplift at the interface is seldom involved in most existing theories of composite beam. At the same time, the existing theoretical formulas are complex and hardly to promote, they are just for scientific research. The element stiffness equation of steel-concrete composite beams considering the slip and vertical uplift effect at the interface has not been discovered in the widely used finite element theories.

In this paper, the finite element solutions of composite beams considering interface slip and vertical uplift of steel girder and concrete slab under the vertical load is deduced based on elastic mechanics and contact theory. This method is not restricted by load and supporting conditions and it is convenient to be applied in practical engineering. A simple and quick calculation theory to the engineering design problem of composite steel-concrete beams is provided.

### 2. BASIC ASSUMPTIONS

According to the actual deformation and loading status of composite steel-concrete beams, the basic assumptions are as follows: (1)Steel girder and concrete slab conform to plane cross-section assumption, respectively; (2)There is vertical displacement difference between steel girder and concrete slab; (3)There is horizontal slip at the interface of steel girder and concrete slab; (4)The horizontal shear stress and the vertical stress transferred at the interface are proportional to the relative displacement difference between the lower edge of concrete slab and upper edge of steel girder.
3. DERIVATION OF THE ELEMENT STIFFNESS MATRIX

3.1. Selection of the Displacement Mode

From Fig. (1), in order to obtain the element deformation model for the composite steel-concrete beams, it is needed to determine the nodal degrees of freedom of the element according to the actual deformation characteristics of composite beams. According to assumptions (2) and (3), there are different vertical displacements, horizontal displacements and different angles between two beam elements. Therefore, the independent degrees of freedom on each node of composite beam element will be six, i.e. the axial displacements of the concrete slab and the steel beam \( u_c \) and \( u_s \); the vertical displacements of the concrete slab and the steel beam \( v_c \) and \( v_s \); the angles of rotation at concrete slab and the steel beam \( \theta_c \) and \( \theta_s \). Thus, the node displacement vector of the composite beam is Eq.(1).

\[
\mathbf{q}^e = \begin{bmatrix} u_{1c} & v_{1c} & \theta_{1c} & u_{1s} & v_{1s} & \theta_{1s} & u_{2c} & v_{2c} & \theta_{2c} & u_{2s} & v_{2s} & \theta_{2s} \end{bmatrix}^T
\]  

where the subscript ‘1’ and ‘2’ represent the left and the right node, respectively.

When the number of nodal degrees of freedom is determined, the displacement mode of the element can be set down. The axial displacement and the vertical displacement use quadratic function and quartic function, respectively, are Eqs.(2) ~ (4).

\[
v_c = c_1 + c_2 x + c_3 x^2 + c_4 x^3 + c_5 x^4
\]  

\[
\theta_c = v'_c = c_2 + 2c_3 x + 3c_4 x^2 + 4c_5 x^3
\]  

\[
u_c = c_{10} + c_{11} x + c_{12} x^2
\]

where \( x \) is axial coordinates of elements, \( c_1 \sim c_5, c_{10} \sim c_{12} \) are undetermined coefficients.

The internal forces can be obtained according to the relationships between the internal forces and displacements [3] as Eqs.(5) ~ (9).

\[
N_c = E_c A_c u'_c = E_c A_c (c_{11} + 2c_{12} x)
\]  

\[
M_c = E_c I_c v''_c = E_c I_c (2c_3 + 6c_4 x + 12c_5 x^2)
\]  

\[
Q_c = M'_c = E_c I_c v^{(3)}_c = E_c I_c (6c_4 x + 24c_5 x)
\]  

\[
q_{uc} = N'_c = E_c A_c u''_c = E_c A_c 2c_{12}
\]  

\[
q_{vc} = Q'_c = E_c I_c v^{(4)}_c = E_c I_c 24c_5
\]

where \( N_c \) is axial force of concrete slab, \( M_c \) is the bending moment undertaken by concrete slab, \( Q_c \) is the shear force undertaken by concrete slab, \( q_{vc} \) is the vertical uplift force at interface, \( q_{vc} \) is the horizontal shear force at interface, \( E_c \) is
The elastic modulus of concrete, \( E_c \), is the inertia moment of concrete slab, \( I_c \), means partial derivative of \( x \). \( (n) \) means \( n \) order partial derivative of \( x \).

Set

\[
\begin{align*}
\psi'' &= \alpha \psi'' = 2\alpha c_{12} \\
\phi^{(4)} &= \beta \phi^{(4)} = 24\beta c_5
\end{align*}
\]  

Integrating Eqs.(10) and (11) yields Eqs.(12) ~ (17).

\[
\begin{align*}
\psi' &= 2\alpha c_{12} x + c_{13} \\
\psi &= c_{12}\alpha x^2 + c_{13}x + c_{14}
\end{align*}
\]  

and

\[
\begin{align*}
\phi^{(3)} &= 24\beta c_5 x + c_6 \\
\phi' &= 12\beta c_5 x^2 + c_6 x + c_7 \\
\phi &= 4\beta c_5 x^3 + \frac{c_6}{2} x^2 + c_7 x + c_8 \\
\phi &= c_5\beta x^4 + \frac{c_6}{6} x^3 + \frac{c_7}{2} x^2 + c_8 x + c_9
\end{align*}
\]

According to the relationships between the internal forces and the displacements as Eqs.(18) ~ (22).

\[
\begin{align*}
N_s &= E_s A_s \psi' = E_s A_s (\alpha 2c_{12} x + c_{13}) \\
M_s &= E_s I_s \psi'' = E_s I_s (\beta 2c_5 x^2 + c_6 x + c_7) \\
Q_s &= M_s' = E_s I_s \psi^{(3)} = E_s I_s (\beta 24c_5 x + c_6) \\
q_{us} &= q_{us} = -N_s' = -E_s A_s \psi'' = -E_s A_s \alpha 2c_{12} \\
q_{vs} &= -Q_s' = -E_s I_s \psi^{(4)} = -E_s I_s \beta 24c_5
\end{align*}
\]

where \( N_s \) is the axial force of steel beam, \( M_s \) is the bending moment undertaken by steel beam, \( Q_s \) is the shear force undertaken by steel beam, \( q_{us} \) is the vertical uplift force at interface, \( q_{vs} \) is the horizontal shear force at interface, \( E_s \) is the elastic modulus of steel, \( I_s \) is the inertia moment of steel beam.

The vertical stresses at the interface are equal, i.e. Eq.(23).

\[
q_{ws} = q_{us}, \quad q_{vs} = q_{us}
\]

Substituting Eqs. (8), (21) and Eqs. (9), (22) into Eq.(23) obtains Eq.(24).

\[
\alpha = -\frac{E_s A_s}{E_c A_c}, \quad \beta = \frac{E_s I_s}{E_c I_c}
\]

After substituting \( \alpha \) and \( \beta \) into Eqs.(13) and (17) we will get the following formulas as Eqs.(25) ~ (27).
3.2. The Displacement Relationship of the Composite Beams

The horizontal displacement at the cross section of the composite beam is depicted in (Fig. 2).

\[ u_s = -\frac{E_A}{E_A} c_{12} x^2 + c_{13} x + c_{14} \quad (25) \]

\[ v_s = -\frac{E l}{E_I c} 6 c_5 x^4 + \frac{c_6}{6} x^3 + \frac{c_7}{2} x^2 + c_8 x + c_9 \quad (26) \]

\[ \theta_s = -\frac{E l}{E_I c} 4 c_5 x^3 + \frac{c_6}{2} x^2 + c_7 x + c_8 \quad (27) \]

From Fig. (2), the expression of the horizontal displacement difference can be obtained as Eq.(28).

\[ \Delta u = u_s - u_c + h_1 \theta_s + h_2 \theta_c \quad (28) \]

The relationship between the displacement difference and the stress of interface is Eq.(30).

\[ q_v = k_1 \Delta v / l \]
\[ q_u = k_2 \Delta u / l \]

\[ \Delta v = v_c - v_s \quad (29) \]

\[ \theta_v = \theta_s \quad \theta_u = \theta_c \quad (30) \]

The vertical stiffness of bolt can be calculated by the method in Ref [15] as Eq.(31):

\[ k_1 = \frac{E_s A_{s p}}{l_{sp}} \quad (31) \]

Where \( E_s \) is the Young’s modulus of the bolt, \( A_{s p} \) is the cross sectional area of the bolt, \( l_{sp} \) is the length of the bolt.

The shear stiffness of bolt can be calculated by the method in Ref [6] as Eq.(32), (33).
\[ k_2 = V_a \times \left(1 - e^{-0.704}\right)^{0.4} \]  
\[ V_a = 1.5 \times A_s \times \sqrt{E_c \times f_{ck} \times n_s} \]

$f_{ck}$ is the prismatic compressive strength of concrete, $A_s$ is the cross section area of bolt, $E_c$ is the Young’s modulus of concrete, $n_s$ is the column number of bolts.

Substituting Eqs. (28), (29) into (30) and setting $l = 1$ arrives at Eqs.(34) and (35).

\[ q_c = k_1 \Delta v = k_1 (v_c - v_s) \]  
\[ q_s = k_2 \Delta u = k_2 (u_s - u_c + h_2 \theta_s + h_2 \theta_c) \]

### 3.3. Determination of the Element Displacement Matrix

The 12 boundary conditions of the constraint element are shown in Eq.(36).

\[ u_c(0) = u_{c1}, \quad u_c(l) = u_{c2}, \quad v_c(0) = v_{c1}, \quad v_c(l) = v_{c2}, \quad \theta_c(0) = \theta_{c1}, \quad \theta_c(l) = \theta_{c2}, \]
\[ u_s(0) = u_{s1}, \quad u_s(l) = u_{s2}, \quad v_s(0) = v_{s1}, \quad v_s(l) = v_{s2}, \quad \theta_s(0) = \theta_{s1}, \quad \theta_s(l) = \theta_{s2}. \]

Simultaneous (34),(35) and (6),(19) respectively, then substitute midpoints into them as Eqs.(37) and (38):

\[ E_c I_c 24 c_3 = \frac{k_1 (v_{c1} - v_{s1} + v_{s2} - v_{c2})}{2} \]  
\[ E_c A_c 2c_12 = \frac{k_1 (u_{s1} - u_{c1} + h_2 \theta_{s1} + h_2 \theta_{c1})}{2} + \frac{k_2 (u_{s2} - u_{c2} + h_2 \theta_{s2} + h_2 \theta_{c2})}{2} \]

Substituting Eqs.(27)–(32) into Eq.(36), and combining with Eqs.(37) and (38), one can solved the coefficients as Eq.(39).

\[ c_1 = v_{c1}, \quad c_2 = \theta_{c1}, \quad c_3 = \frac{3v_{c1} - \theta_{c1} l - 3v_{s1} - 2\theta_{s1} l}{l^2} + \frac{k_1 l (v_{c1} - v_{s1} + v_{s2} - v_{c2})}{48E_c I_c}, \]
\[ c_4 = \frac{\theta_{c1} l + 3\theta_{s1} l + 2v_{c1} - 2v_{s1}}{l^3} - \frac{k_1 l (v_{c1} - v_{s1} + v_{s2} - v_{c2})}{24E_c I_c}, \quad c_5 = \frac{k_1 (v_{c1} - v_{s1} + v_{s2} - v_{c2})}{48E_c I_c}, \]
\[ c_6 = \frac{6v_{s1} - 2\theta_{s1} l - 4\theta_{s1} l - 6v_{s1} + k_1 (v_{c1} - v_{s1} + v_{s2} - v_{c2}) l}{4E_c I_c}, \]
\[ c_7 = \frac{6v_{s2} - 4\theta_{s1} l - 6\theta_{s1} l - 6v_{s1} - k_1 (v_{c1} - v_{s1} + v_{s2} - v_{c2}) l}{4E_c I_c}, \]
\[ c_8 = \theta_{s1}, \quad c_9 = v_{s1}, \quad c_{10} = u_{c1} \]
\[ c_{11} = \frac{u_{s1} - u_{c1}}{l} - \frac{k_1 l}{4E_c A_c} \left[ (u_{s1} - u_{c1} + h_2 \theta_{s1} + h_2 \theta_{c1}) + (u_{s2} - u_{c2} + h_2 \theta_{s2} + h_2 \theta_{c2}) \right], \]
\[ c_{12} = \frac{k_2}{4E_c A_c} \left[ (u_{s1} - u_{c1} + h_2 \theta_{s1} + h_2 \theta_{c1}) + (u_{s2} - u_{c2} + h_2 \theta_{s2} + h_2 \theta_{c2}) \right], \]
\[ c_{13} = \frac{u_{s2} - u_{c2}}{l} + \frac{k_1 l}{4E_c A_c} \left[ (u_{s1} - u_{c1} + h_2 \theta_{s1} + h_2 \theta_{c1}) + (u_{s2} - u_{c2} + h_2 \theta_{s2} + h_2 \theta_{c2}) \right], \]
\[ c_{14} = u_{s2} \]
Take (39) back into the trial function and show with the form of matrix as Eq.(40):

\[
\begin{pmatrix}
\kappa_u = 
\begin{bmatrix}
(1 - \frac{v}{2}) h_{xx}^2, h_{xx} h_{yy}, 0, h_{xx} h_{yy}, h_{yy}^2
\end{bmatrix}^T \\
\kappa_v = 
\begin{bmatrix}
0, h_{xx} h_{yy}, h_{xx} h_{yy}, h_{yy}^2
\end{bmatrix}^T \\
\kappa_w = 
\begin{bmatrix}
0, h_{xx} h_{yy}, h_{xx} h_{yy}, h_{yy}^2
\end{bmatrix}^T \\
\end{bmatrix}
\]

(40)

3.4. Elemental Generalized Strain Matrix and Generalized Force Matrix

By the basic principles of elastic mechanics as Eq.(41).

\[
\begin{bmatrix}
\kappa_u'(x) = \nu
\\
\kappa_v'(x) = \frac{\partial u}{\partial x}
\end{bmatrix}
\]

(41)

Where \( \kappa_u(x) \) and \( \kappa_v(x) \) is the horizontal strain. Taking the derivatives of Eq.(40) yields Eq.(42).

\[
\begin{bmatrix}
\kappa_u'(x) = 
\begin{bmatrix}
(1 - \frac{v}{2}) h_{xx} h_{yy}, h_{xx}^2, h_{xx} h_{yy}, h_{xx} h_{yy}, h_{yy}^2
\end{bmatrix}^T \\
\kappa_v'(x) = 
\begin{bmatrix}
0, h_{xx} h_{yy}, h_{xx} h_{yy}, h_{yy}^2
\end{bmatrix}^T \\
\kappa_w'(x) = 
\begin{bmatrix}
0, h_{xx} h_{yy}, h_{xx} h_{yy}, h_{yy}^2
\end{bmatrix}^T \\
\end{bmatrix}
\]

(42)

Equation (42) can be denoted as Eq.(43).

\[
\begin{bmatrix}
\epsilon_u(x) \\
\epsilon_v(x) \\
\epsilon_w(x)
\end{bmatrix}
= [\kappa'] \begin{bmatrix} q' \end{bmatrix}
\]

(43)

where \( B \) is the generalized strain matrix.

By the physical equations of the beam as Eq.(44):

\[
\begin{align*}
N_{uu} &= E_A \epsilon_u(x) \\
M_{uv} &= E_I \kappa_u(x) \\
N_{ww} &= E_A \epsilon_w(x) \\
M_{ww} &= E_I \kappa_w(x)
\end{align*}
\]

(44)
where $E_c$ and $E_s$ are the Yong’s modulus of concrete slab and steel girder, respectively; $I_c$ and $I_s$ are second moment of area of concrete slab and steel girder, respectively.

Substituting Eq. (42) into Eq. (44) yields Eq.(45).

\[
N_m = \left[ \begin{array}{c}
0 \\
0 \\
0 \\
0 \\
0 \\
0 \\
0 \\
0
\end{array} \right] = \left[ \begin{array}{c}
0 \\
0 \\
0 \\
0 \\
0 \\
0 \\
0 \\
0
\end{array} \right] = Nq^e
\]

Equation (45) can be denoted as Eq.(46).

\[
\sigma = \begin{bmatrix}
N_c \\
M_{ce} \\
N_{ec} \\
M_{ec}
\end{bmatrix} = Nq^e
\]

where $N$ is the generalized force matrix.

3.5. The Expression of Element Stiffness Matrix

Set the nodal force vector of the element as Eq.(47).

\[
F^e = \begin{bmatrix}
N_{1c} \\
N_{1s} \\
M_{1c} \\
M_{1s} \\
N_{2c} \\
N_{2s} \\
M_{2c} \\
M_{2s}
\end{bmatrix}^T
\]

The total potential energy of element is Eq.(48).

\[
\pi = \frac{1}{2} q^e \left( \int_0^1 B^T N dx \right) q^e - q^e^T F^e
\]

According to the principle of minimum potential energy, make the first variation of the potential energy function of the system equal to zero AS Eq.(49).

\[
q^e = q^e_0 K^e q^e - q^e_0 q^e_0 F^e = 0
\]

From Eq.(49), the static equation of the beam can be obtained as Eq.(50).

\[
K^e q^e - F^e = 0
\]

where $K^e = \int_0^1 B^T N dx$ is the element stiffness matrix, which can be expressed explicitly as Eq.(51) and (52).

\[
K^e = \begin{bmatrix}
k_{11} & k_{12} & k_{13} \\
k_{21} & k_{22} & k_{23} \\
\text{symmetry}
\end{bmatrix}
\]

where
where $\delta$ is the original equivalent load vector, $K$ is the global stiffness matrix, $P$ is the original equivalent load vector, $\delta$ is the nodal displacement vector.

**4. SOLUTION OF THE NODE DISPLACEMENT MATRIX**

The global stiffness equation of structure can be obtained from literature [21 - 23] as Eq.(53).

$$K\delta = P$$

(53)
The global stiffness matrix $K$ and the original equivalent load matrix $P$ can be obtained by assembling the element stiffness matrix $K_e$ and the equivalent load matrix $P_e$ that already obtained as Eqs.(54) and (55). When the load is uniformly distributed load $q$

$$P^u = \begin{bmatrix} 0 & \frac{qL^2}{2} & 0 & 0 & 0 & 0 & 0 & 0 & \frac{qL^2}{2} & 0 & 0 & 0 \end{bmatrix}^T$$

(54)

when the load is concentrated load $p$

$$P^c = \begin{bmatrix} 0 & \frac{pL}{2} & 0 & 0 & 0 & 0 & 0 & 0 & \frac{pL}{2} & 0 & 0 & 0 \end{bmatrix}^T$$

(55)

The node displacement matrix $\delta$ can be obtained by substituting them processed by multiplied with bigger number method into Eq.(53).

5. EXAMPLE OF VERIFICATION AND ANALYSIS

In order to demonstrate the correctness of the presented method for calculating the slippage and uplift of composite steel-concrete beams, two composite beams with their sectional dimensions shown in Fig. (1) were tested and calculated. The span of this composite beams is 4.0m and the size of concrete slab is 800mm × 80mm, the size of steel roof is 120mm × 6mm, the size of the steel web is 6mm × 238mm, the size of the steel bottom slab is 120mm × 6mm. The diameter of bolt is 12mm and the arrangement form of bolts is double row and symmetrical, the spacing of each row is 60mm, along the beam length direction bolts was uniform arranged and the spacing was 200mm of each row. Concrete grade of roof is C40 and the steel grade of steel girder is Q335, the performance level of bolt is 6.5. 50kN concentrated loads were applied at 1.4m from the beam at both ends. The model has 40 units. The calculation time is 3minutes.

The comparisons of the results calculated by the presented method and the experimental results are shown in (Figs. 3-6).

![Graph](image)

Fig. (3). The contrast of calculated value and experimental value of deflection.
By comparison, the results of calculation got by the method of the new type of bar system finite element and testing are in good agreement. Both deflection and slip strain difference are shown in Figs. (3 and 4). As shown in Fig. (3), the values of midspan deflection obtained from test 1 and test 2 are 6.07mm, and the calculated value is 6.20mm. The relative error between the results of calculation and testing is 2% at most. Fig. (4) shows that slip strain difference presents M-shape along the beam, and the curve is symmetrical. It should be noted, there are some discrepancies between the results of calculation and testing of slip strain difference, the possible reasons may be the existence of test errors, which mainly from the positions of studs and the sticking positions of strain gauges. It can be proved that element stiffness matrix derived in this article is correct. At the same time calculated results of relative slippage and the value of vertical lift can be obtained quickly and accurately by using the calculation method, perfecting the calculation theory of composite beams that only considering slip effect. According to the results shown in Figs. (5-6), the uplift has almost the same order of magnitude of shear slip near the beam ends, however in the central region of the beam, it is almost zero. It shows that uplift is relevant and can't be ignored, especially when flexible shear connectors are provided between steel girder and concrete slab. Due to the deformation of flexible shear connectors, it can only play a part of the horizontal shear and vertical uplift effect. And it must be said that the element is not able to take into account the shear-lag effect, which can be necessary to evaluate the effective width. The method can be obtained from Ref [24].
CONCLUSION

1. The finite element solution of composite steel-concrete beams considering the existence of interface slip and vertical uplift is derived for the first time based on elastic mechanics and contact theory which solves the problem of slip and uplift at the interface of composite beams using common finite element method.
2. Comparing the results of calculation and test results of composite steel-concrete beams, the correctness of the finite element of composite beams derived in this paper was assessed.
3. The finite element method is feasible and effective. The element stiffness matrix was derived in this paper. It can be seamlessly integrated into the current engineering design software and provide effective help to practical engineering problems. It can not only be used to calculate the displacement and stress of steel-concrete composite beams under vertical loads, but also can calculate inner force and distortion of bridge deck pavement casted by stages under the vehicle loads. It provides an accurate calculation method for the large span beam-type structure with steel-concrete composite beams.

CONFLICT OF INTEREST

The author confirms that this article content has no conflict of interest.

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Declared none.

REFERENCES


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