The Optimization Model and Algorithm for Train Connection at Transfer Stations in Urban Rail Transit Network

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Abstract: In urban rail transit network, the passenger transfer time depends on the train connection states in transfer stations, so the optimization of the connection relations of arrival and departure time among trains is significant to improve the level of transfer service. Here, with the psychology of waiting passengers taken into consideration, the cost function of transfer waiting times has been established. On this basis, an optimization model for train connections at transfer stations was constructed, and a genetic algorithm was designed to solve this model. A computer program implementing this genetic algorithm was written in Microsoft VB.NET. And the program is used to optimize the train operation plans of a simple network which consists of four urban rail lines in Beijing. The results show that the proposed method can effectively reduce the total waiting time cost of all transfer passengers in the network.

Keywords: Genetic algorithm, train connection optimization, transfer, urban rail transit network.

1. INTRODUCTION

With the expansion of the urban rail transit network, the number of transfer nodes on passenger travel routes has increased substantially, and transfer has become a necessary step in most rail travels. To provide safe and efficient transfer service is key to improving the overall service level of the rail transit network. The time required for transfer is a direct manifestation of transfer efficiency, and also directly reflects the level of the rail network management. Previous studies on rail transfers have focused largely on transfer station design and on transfer stream design in order to minimize the passenger walking time during transfer. However, restricted by a variety of objective conditions, the room for reducing the transfer walking time is rather limited. In addition, compared to reducing the walking time, reducing the transfer waiting time is more valuable to passengers. The transfer waiting time is directly associated with the arrival and departure times of trains taken before and after the transfer at the transfer station. Thus, Coordinating and optimizing the train schedules of different lines connected by transfer stations can make the arrival and departure times of trains realize optimal connections, thereby successfully reducing the transfer waiting time of passengers at the program level.

At present, in most major cities the train schedules are compiled using the method of “making schedules by line and adjusting schedules at the network level.” More accurately, the schedules are first crafted at the level of individual lines in accordance with passenger demand and transport capacity resources; train schedules of different lines are compiled separately. Then, at the network level, adjustments are made from the perspective of coordination and overall benefits. However, with this method, once the train schedules are completed, it is difficult to change factors, such as number of running trains, intervals and dwelling times, and adjustments can only be made within a very narrow margin. Furthermore, because of the complex coupling relationships between lines, the complexity of which increases as the network scale expands, the adjustment of some single point will exert time propagation effects on the entire network, which further limits the impact of the adjustment. Therefore, we believe that the current method of compiling train schedules does not take into account the collaborative relationship between lines, directly leading to an increase in passenger waiting time in the transfer stations within the network. This has created a bottleneck at the service level of the rail transit network.

Based on the existing results and issues, this paper treats the train system as a black box and uses global coordination as the guideline to develop an optimization model for train connections at transfer stations. The goal is to achieve mutual coordination between the train schedules of different lines. The effectiveness of the optimization method has been verified using a specific example.

2. LITERATURE REVIEW

With the expansion of the urban public transport network, there has been continued growth in the proportion of time spent by passengers at the transfer nodes during their overall travel time. Therefore, the coordination and optimization of transit timetables (schedules) targeting the optimization of transfer waiting times has received wide attention from researchers. For a systematic review of the existing
literature, the previous research will be divided into three series according to the object of study, and then summarized. In the first series, transfer nodes in the regular bus system will be the object of study; in the second series, the object of study is the transfer hubs in the urban public transit system, consisting of regular bus and rail transit system; in the third series, the object of study is the transfer nodes in the urban rail transit system.

The first and second series investigated how to achieve efficient connections between buses in different lines or between buses and trains at the transfer station via optimization of the bus timetables. The preparation of train timetables is different from that of bus timetables primarily due to the following reasons. First, rail transit is limited by the train running intervals; also, the running time in the section, the dwelling time in the station and the departure interval are all relatively fixed, tolerating only small fluctuations. Methods for optimizing the bus timetables cannot be directly applied to rail transit. In addition, to improve the success rate of transfers at the same platform and under the condition of transfers through tunnels, and designed a heuristic algorithm to solve the model. Moreover, to solve the coordination between transfer nodes in the network, studies in the third category artificially set the importance of the transfer stations and lines, thereby determining the priority in the coordinative optimization between different transfer stations and lines. This provides a method for resolving the conflict between the train connection schedules for different transfer stations; however, it is too subjective and may generate closed-loop connections that have contradictions. More importantly, with this method the obtained network train schedules are not the optimal solution.

From the existing research results in this field, the following conclusions can be drawn as follows. First, the current coordination of network transit timetables (operation charts) targeting the optimization of transfer connections has mostly focused on the optimization of regular bus timetables. Yet vehicle management of regular buses is greatly different from that of rail transportation, and hence the method used for optimizing regular bus schedules cannot be directly applied to rail transit.

Second, the number of published studies on train connection optimization targeting urban rail transit networks is relatively small. To achieve the optimization of train connections at all transfer stations within the network, all train schedules must be prepared with the global network taken into consideration from the start, rather than merely making coordinative adjustments on existing train timetables prepared separately by lines. This is the fundamental difference between the present study and all previous studies. Meanwhile, previous studies typically used the minimization of the transfer wait times as the optimization objective, yet the
transfer wait time is not entirely inversely proportional to passenger satisfaction. In fact, it has been shown that when the waiting time is less than 30s, the degree of passenger dissatisfaction is highest [6]. Therefore, the present paper considers the psychology of waiting passengers and converts the transfer waiting time into the transfer cost. Minimization of the transfer cost is set as the objective to construct the optimization model for train connections at transfer stations in urban rail transit systems.

3. ASSUMPTIONS

This study is based on the following assumptions:

1. The transport configuration of all lines in the network can meet passenger demand, and the facility capacities of all transfer stations can also meet passenger demand.
2. The running times in the section, the dwelling times in the station, train running intervals and transfer walking times at all transfer stations are all known input parameters.
3. The passenger transfer demand is relatively stable over a period of time.
4. After arriving at the platform for the connecting direction, all transfer passengers take the first available connecting train.
5. Transfer between the up-bound and down-bound directions in the same line is not taken into consideration.
6. There is no joint operation between lines, and for lines with multiple routes only one route is considered.
7. The isolated lines in the network are not considered in the optimization model.

4. THE ESTABLISHMENT OF THE OPTIMIZATION MODEL

4.1. Problem Analysis

Under the premise that basic train operation data, such as running times in the section, dwelling times in the station, train running intervals, are determined, the train schedule of one certain line in the coordination time period is determined by the departure time of the first train in this time period. Let the coordination time period be \([t_0, t_1]\), the departure time of the first train is a time point at \([0, h]\) \((h \text{ is the train running interval)}\) after the starting time point of the coordination period \(t_0\). In other words, the time interval between the departure time of the first train and \(t_0\) is a variable in \([0, h]\).

Under the assumption that there is no joint operation between lines, the train schedules of different lines are independent of each other. Because loop routing is usually used in urban rail transit systems, the train schedules of up-bound train and down-bound train of the same line are closely associated with each other. For each line, after the train schedule in one direction within the coordination time period is set, the schedule of the trains in the other direction is also determined. Hence, in this paper the objects of train connection optimization is restricted to one direction of each line in the network; this direction is called the coordination direction. In this way, the decision variables of the optimization model become the time intervals between \(t_0\) and the departure time of the first train of various lines’ coordination direction within the network in \([t_0, t_1]\).

The goal of train connection optimization is to achieve the rational connections of trains from different lines at the transfer stations, thereby reducing the cost of passengers’ transfer waiting times. Therefore, the objective function of the optimization model is the minimization of the total cost of passengers’ transfer waiting times at all transfer stations in the network.

4.2. The Cost Function Corresponding to the Transfer Waiting Time

The transfer waiting time is the time interval between the point when the passenger arrives at the platform of the connecting line and the point when the passenger boards the connecting train. If the connecting train arrives just as the passenger is arriving at the platform of the connecting line, the passenger’s transfer waiting time is 0; if the connecting train has just departed, the passenger’s transfer waiting time is close to the difference between the running interval of the connecting train and the stop time of the connecting train at this particular transfer station. These are the two extremes of the transfer status. The latter is the worst scenario for the passenger, because the transfer waiting time is the longest; however, the former scenario is not ideal either. A survey has shown that when the transfer waiting time is less than 30s, the dissatisfaction degree of transfer passenger is rather high [6]. The main reason for this is that a tight connection time will create the psychological pressure of a potentially missed connection on transfer passengers; this sense of crisis is particularly evident when the train running frequency is low. Thus, this paper introduces the concept of a comfortable passenger waiting time, which is the waiting time that satisfies the passenger’s psychological comfort. The optimal transfer status refers to a situation in which the transfer waiting time exactly equals the comfortable passenger waiting time.

Next, the cost function \(C(t)\) corresponding to the transfer waiting time will be established. The cost corresponding to the comfortable passenger waiting time is minimum; the cost is increased when the transfer waiting time is greater or smaller than the comfortable passenger waiting time. Thus the following function is used (function plot shown in Fig. (1):

\[
C(t) = \begin{cases} 
C_1 \frac{C_2}{RT} \times t, & t < RT; \\
\frac{C_2}{h} \left( \frac{1}{RT} - \frac{1}{RT_con} \right) \times (t - RT), & t \geq RT.
\end{cases}
\]

where,

\(t \) --- the transfer waiting time, min;
RT --- the comfortable passenger waiting time, min;

\( h_{\text{con}} \) --- the running interval of the connecting train, min;

\( DT_{\text{con}}^{a} \) --- the stop time of the connecting train at the transfer station \( a \), min;

\( C_{1}, C_{2} \) --- coefficients.

The values of coefficients \( C_{1} \) and \( C_{2} \) can be determined by the passenger travel time value. The waiting time of 0 will bring the passenger a certain psychological sense of crisis, which is equivalent to the generation of a certain time cost, i.e. \( C_{1} \).

Here the value of the time the passenger spends waiting after having boarded the train is used to determine the value of coefficient \( C_{1} \). Parameter \( C_{2} \) describes the cost of waiting time when the passenger just misses the expected connecting train.

In public transportation, the value of the waiting time is often determined relative to the value of the riding time [5]. The per unit riding time value is set to 1, denoting the value of unit time that the passenger spends on the running train. Then, the per unit value of time that the passenger spends on the platform waiting for the train is set to 2.5, meaning that the time cost of riding for 2.5 min is equivalent to that of waiting on the platform for 1 min. If the worst transfer status occurs, the passenger will wait for a period of about \( h_{\text{con}} - DT_{\text{con}}^{a} \). In this case, the psychological anxiety of waiting is enhanced, leading to increased time value; the per unit waiting time value in this case is set to 2.7 [5]. Compared to waiting on the platform, a passenger waiting inside the train is more comfortable, and the value of unit time spent on waiting in the train is set to 2. Thus here we set \( C_{1} = 2DT_{\text{con}}^{a} \) and \( C_{2} = 2.7\left(h_{\text{con}} - DT_{\text{con}}^{a}\right) \).

### 4.3. Mathematical Model

According to the above analyses, targeting the coordination time period \( [t_{i}, t_{j}] \), the following optimization model for train connections at transfer stations in urban rail transit networks is constructed:

\[
\min F(X) = \sum_{s=1}^{n} \sum_{j=1}^{s} \sum_{i=1}^{s} C(t_{i,j,s}(X)) \times V_{i,j,s}
\]

s.t. \( X = (x_{1}, x_{2}, \cdots, x_{n}) \times x_{s} \in [0, h_{s} - 1] \) and \( x_{s} \in N \); \( 1 \leq k \leq n \) (3)

\[
C(t_{i,j,s}(X)) = \begin{cases} 
2DT_{\text{con}}^{a} - \frac{t_{i,j,s}(X)}{RT} & , t_{i,j,s}(X) < RT \leq \sqrt{h_{\text{con}} - DT_{\text{con}}^{a} - RT} \\
2.7 \times \frac{RT}{h_{\text{con}} - DT_{\text{con}}^{a} - RT} & , t_{i,j,s}(X) \geq RT 
\end{cases}
\]

where,

\( X \) --- the decision variable. It is an \( n \)-dimensional vector;

\( n \) is the number of lines in the network (isolated lines not included);

\( x_{s} (1 \leq k \leq n) \) --- the time interval between \( t_{k} \) and the departure time of the first train of line \( k \)'s coordination direction in the time period \( [t_{0}, t_{1}] \), and \( x_{s} \) is a natural number in the interval \( [0, h_{s} - 1] \), min;

\( h_{s} \) --- the running interval of line \( k \), min;

\( t_{i,j,s}(X) \) --- the transfer waiting time of the \( s \)th batch of transfer passengers in the \( j \)th transfer connection at the \( i \)th transfer station in the time period \( [t_{0}, t_{1}] \) and under the network train schedules corresponding to \( X \) (min)(a transfer connection describes a transfer from up-bound/down-bound of a feeder line to up-bound/down-bound of a connecting line);

\( C(t_{i,j,s}(X)) \) --- the cost function corresponding to the transfer waiting time \( t_{i,j,s}(X) \);

\( DT_{\text{con}}^{a} \) --- the stop time of the connecting train in the \( j \)th transfer connection at the \( i \)th transfer station;

\( h_{\text{con}}^{i,j} \) --- the running interval of the connecting train in the \( j \)th transfer connection at the \( i \)th transfer station;

\( V_{i,j,s} \) --- the total number of the \( s \)th batch of transfer passengers in the \( j \)th transfer connection at the \( i \)th transfer station;
station in the time period \([t_0, t_1]\). It is estimated according to
the statistics on passenger volume in this time period at the
transfer station, and based on the assumption that within the
time window of statistics, the numbers of passengers in dif-
ferent batches are the same;

\[ m \] ---the number of transfer stations in the network;

\[ r_i \] ---the number of transfer connections at the \(i\) th trans-
fer station; \( r_i = \left(2n_i^l + n_i^r\right) - \left(4n_i^l + n_i^r\right) \), where \( n_i^l \) and \( n_i^r \) rep-
resent the number of lines passing through and ending at
the \(i\) th transfer station.

\[ g_{i,j} \] ---the number of batches of passengers in the \(j\) th
transfer connection at the \(i\) th transfer station in the time
period \([t_0, t_1]\); \( g_{i,j} = \frac{t_j - t_0}{h_{f,j}} \), where \( h_{f,j} \) repre-
ts the running interval of the feeder train in the \(j\) th transfer
connection at the \(i\) th transfer station.

5. DESIGN OF THE OPTIMIZATION ALGORITHM

5.1. Methods for Solving the Optimization Model

In the optimization model, it is difficult to express the
mapping from decision variable \(X\) to the transfer wait time
\(t_{i,j,k}(X)\) using mathematical formulas. Therefore, the model cannot be solved with traditional ana-
lytical methods.

Meanwhile, Different element combinations of \(x_k\)
\((1 \leq k \leq n)\) form the feasible region of \(X\), and the number
of feasible solutions is \(\prod_{k=1}^{n} h_k\). Take the currently operating
Shanghai rail transit network for example. It contains 14
lines. In the simplest scenario, assuming the running inter-
vals of all lines in the coordination time period are 5min,
then the number of feasible solutions reaches
\(2^{14} = 6103515625\). Thus, it is difficult to simply apply an
exhaustive search method to find the optimal solution. A
heuristic algorithm is most commonly used to solve this type of
problem. Here a genetic algorithm has been used to solve the
optimization model.

5.2. The Steps of the Genetic Algorithm

The overall steps of the genetic algorithm are as follows:

1. The initial population is randomly generated, and the
initial generation of individuals is obtained. Each individual is represented as gene encoding of the chromosome.

2. The fitness of each individual is calculated.

3. The fitness, gene encoding and function value of the individual with the maximum fitness in the current gen-
eration are all recorded.

4. Determine whether the condition for stopping evolution
is satisfied; if yes the calculation is stopped here, other-
wise the evolution continues.

5. Regenerating individuals are selected according to fit-
ness; individuals with high fitness have a high proba-
ability of being selected, whereas those with low fitness are
likely to be eliminated.

6. According to certain crossover probabilities and cross-
over methods, new individuals are generated.

7. According to certain mutation probabilities and mutation
methods, new individuals are generated. The new gen-
eration of population is thus obtained, and the loop re-
turns to step 2.

5.3. The Key to the Design of the Genetic Algorithm

5.3.1. Encoding and Decoding

The decision variable \(X\) in the optimization model is an integer vector, and can be viewed as the phenotype of the genetic algorithm. The mapping process from the phenotype to the genotype is encoding. This paper uses binary encoding to represent the individual's genotype. The specific encoding and decoding methods are as follows.

One chromosome represents one combination of the in-
tervals between \(t_0\) and the departure time of the first train of
\(n\) lines in \([t_0, t_1]\).

Each chromosome can be divided into \(n\) segments; the bit string in the \(k\) th segment \((1 \leq k \leq n)\) represents the time interval between \(t_0\) and the departure time of the first train
of line \(k\) 's coordination direction in \([t_0, t_1]\). To encode the
bit string in the \(k\) th segment, a binary string encoding
method for integer is used. Let integer \(x_k \in [0, h_k - 1]\)
\((1 \leq k \leq n)\). \(h_k - 1\) is dissociated using the following algo-

\[ n_k = 0; x = h_k - 1; p = 0 \\
\text{do } p = p + 1 \\
\quad n_p = \text{int}\left[\log_2\left(x + 1\right)\right] \\
\quad x = x - 2^{n_p} + 1 \text{ while } x > 0 \\
\]

The \(p\) integers \(n_j (j = 1, 2, \cdots, p)\) generated from the
above algorithm satisfies \(h_k - 1 = \sum_{j=1}^{p} (2^{n_j} - 1)\). Namely,

\(h_k - 1\) is the sum of \(p\) binary numbers with digit number
\(n_j (j = 1, 2, \cdots, p)\). Thus, \(x_k\) can be represented by

\( (n_1 + n_2 + \cdots + n_p) \) binary strings \(B_k\), \(i.e.,
\( x_k = \sum_{j=1}^{p} B_k = \sum_{j=1}^{p} (b_{n_j} \cdots b_{n_2} b_{n_1})_k\), where, \(b\) is the binary bit of 0 or 1.
For example, if \( x_i \in [0, 5] \), after decomposing \( h_i - 1 = 5 \), three integers \( \{n_i = 2, n_2 = 1, n_3 = 1\} \) are obtained, which satisfy \( 5 = (2^2 - 1) + (2^1 - 1) + (2^1 - 1) \). Thus, \( x_i \) can be represented by four-digit binary strings \( b_1 = \left\{ b_i^1, b_i^2, b_i^3, b_i^4 \right\} \), namely \( x_i = \sum_{j=1}^{n_i} b_i^j \).

From the above encoding method, the chromosome decoding method can be obtained. First, the chromosome is divided into \( n \) segments. For \( \forall k \ (k = 1, 2, \ldots, n) \) segment, the binary digits \( n_j + n_2 + \ldots + n_p \) are determined, and the \( p \) binary numbers with the number of digits \( n_j \) \((j = 1, 2, \ldots, p)\) are then converted into decimal numbers. Finally, the decimal numbers are added up to obtain \( x_k \).

For example, consider an urban rail transit network that contains four lines; the coordination time period is 11:00-12:00, and the running intervals of the four lines in the time period are 6min, 7min, 5min and 7min. Chromosome “110111101010110” constitutes a feasible solution. It is divided into 4 segments, and the numbers of digits in the different segments are 4, 4, 3 and 4. Then the binary number in each segment is dissociated to obtain “11 | 0 1 | 11 | 10 | 10 | 01 | 10." Then all the binary numbers are converted into decimal numbers and added together, obtaining \( x_i = 4, x_2 = 5, x_3 = 3, x_4 = 3 \). Thus the departure times of the first train in the coordination direction entering the coordination time period are 11:04, 11:05, 11:03 and 11:03.

5.3.2. Constructing the Fitness Function

The fitness function is normally derived from the objective function, and needs to meet the basic conditions of being single-valued, continuous, non-negative and maximized [11]. Considering that the optimization model is to find the minimum value, and the value range of the objective function is \( [0, +\infty) \), the fitness function can be set as the inverse of the objective function, namely:

\[
\text{Fit}(F(X)) = \left[ F(X) \right]^{-1}
\]

The smaller the value of the objective function, the larger the corresponding fitness value, and the greater the probability of the individual gene being passed on to the next generation. In addition, because the value of the objective function is generally not close to 0, the fitness value determined by formula (5) will not show positive spillover. In the process of calculating the objective function value according to the phenotype of an individual with a certain chromosome, two steps are needed.

The first step is to determine the network train schedules based on the decision variable \( X \) and the known basic operation data of the trains. Two rules that need to be followed during the calculation process are clarified as follows.

First, if the locomotive use cycle is not an integer multiple of train running intervals, the locomotive operation cycle is enlarged by increasing the reentry time, so that the operation cycle becomes an integer multiple of the running intervals. In this way, the train running intervals within the coordination time period remain consistent.

Second, given one solution of \( X = \{x_1, x_2, \ldots, x_n\} \), from \( x_i \) it can be obtained that the departure time of the first train of line \( k \)'s coordination direction in \([t_0, t] \) is \( t_{k1} = t_0 + x_k \).

Then it can be deduced that the departure time of the first train of line \( k \)'s non-coordination direction in \([t_0, t] \) is:

\[
t_{k1} = t_0 + x_k + t_{\text{travelt}} + t_{\text{reentryt}} - r \times h_k
\]

where,

\[
t_{\text{travelt}} \quad \text{--- the travel time of the train of line k \text{'s coordination direction;}
\]

\[
t_{\text{reentryt}} \quad \text{--- the reentry time of trains of line k \text{'s coordination direction;}
\]

\[h_k \] denotes the train running intervals of line \( k \); \( r = \left[ \frac{t_0 + x_k + t_{\text{travelt}} + t_{\text{reentryt}}}{h_k} \right], \) representing the greatest positive integer smaller than \( \frac{t_0 + x_k + t_{\text{travelt}} + t_{\text{reentryt}}}{h_k} \).

The second step is to match train pairs for each transfer relation at all the transfer stations based on the network train schedules, and to then calculate the transfer waiting time of the passengers for each train pair. Next, the corresponding time cost is calculated, and finally all time costs are added to obtain the objective function value \( F(X) \).

5.3.3. Conditions for Stopping the Loop

In this paper, the following three conditions are used to determine if the loop should be stopped.

1. The optimal solution remains unchanged in generation \( GN_{\text{min}} \).
2. In one generation the difference between the best fitness and the worst fitness is smaller than \( \bar{F} \) (%).
3. The greatest number of evolving generations is \( GN_{\text{max}} \).

5.3.4. The Selection, Crossover and Mutation Operators

5.3.4.1. The Selection Operator

Here fitness proportionate selection is used, combined with tournament selection. Fitness proportionate selection is the most basic selection method. The expected number of selections for each individual is associated with the ratio of its fitness value to the mean fitness value of the population. This method is similar to the roulette wheel in a casino. In tournament selection, before executing the selection operation, the individual with the highest fitness value in the parent population is selected as the global best individual; after
completing the selection and crossover operations, the best individual of the current population is selected as the local best individual, and is then compared to the global best individual. The individual with the higher fitness value is then selected as the current global best individual. After one genetic operation is completed, the current global best individual is used to replace the individual with the lowest fitness value in the offspring generation.

5.3.4.2. The Crossover Operator

In this paper uniform crossover has been used; each location on the chromosome bit string was subjected to random uniform crossovers at the same probability. The specific steps are as follows. For one pair of parent individuals, whether the crossover operation needs to be executed is determined according to the crossover probability $c_p$; if yes, a 0-1 mask of the same length as the individual is randomly generated, and various segments of the mask determine which parent provides value for the offspring individual in the corresponding segments, and a new individual is thus generated.

5.3.4.3. The Mutation Operator

The mutation operator is implemented by randomly reversing the binary string of a certain allele according to the mutation probability $p_m$. Specifically, for a given chromosome bit string, $s = a_1a_2\cdots a_L$, the operation is:

$$a_i' = \begin{cases} 1-a_i, & \text{if } x_i \leq p_m \\ a_i, & \text{otherwise} \end{cases}, \quad i \in \{1,2,\ldots,L\}. \quad (7)$$

In this way, the new individual $s' = a_1'a_2'\cdots a_L'$ is generated. $x_i$ is uniform random variable corresponding to each gene locus, $x_i \in [0,1]$.

6. EXAMPLE

To verify the effectiveness of the model and the algorithm, here in the Win7 operating system a program implementing the genetic algorithm was written in Microsoft VB.NET. Using this program, a simple network composed of Line 1, Line 2, Line 5 and Line 13 in Beijing rail transit system (as shown in Fig. 2) was subjected to the optimization of network train operation charts for a certain time period (11:00-12:00).

The basic network data involved in the algorithm (including running times in the section, dwelling times in the station, train running intervals, reentry times, transfer walking times, the volume of transfer passengers, etc.) were set according to the actual operational data of the Beijing rail transit network. The running intervals for each line are shown in Table 1. The values of other relevant parameters are shown in Table 2.

<table>
<thead>
<tr>
<th>Rail Transit Line</th>
<th>Train Running Interval</th>
</tr>
</thead>
<tbody>
<tr>
<td>No. 1</td>
<td>4min</td>
</tr>
<tr>
<td>No. 2</td>
<td>5min</td>
</tr>
<tr>
<td>No. 5</td>
<td>6min</td>
</tr>
<tr>
<td>No. 13</td>
<td>7min</td>
</tr>
</tbody>
</table>

For all lines, the coordination direction is set to be down-bound. The results obtained after running the program are shown in Table 3.

After optimization, the total cost of transfer wait times for all passengers in this rail network from 11:00-12:00 is 30789.66. However, according to the current daily train
schedules, the value of the objective function is 35633.23. Therefore, using the model and the algorithm proposed in the present paper for the optimization of the network train schedules, the value of the objective function was reduced by 13.59%. Thus it is proven that the method proposed in this study is effective.

Because this example only includes 4 lines, the number of feasible solutions is 360; it would be practical to apply the exhaustive search method to obtain the optimal solution. A program implementing the exhaustive search method was then written in Microsoft VB.NET. It was found that the optimal result obtained using the exhaustive search algorithm was the same as that obtained using the genetic algorithm. Hence it is proven that the genetic algorithm proposed in this paper is feasible and effective in solving the optimization model.

CONCLUSION

In order to improve passenger service level of urban rail transit systems under the condition of network operation, the operation management department should coordinate and optimize the network train schedules according to the characteristics of passenger demands in the rail network, promoting rational connection between different lines at the transfer stations. This paper takes the psychology of passenger waiting into consideration and constructs the cost function of transfer wait times. On the basis of meeting the actual transfer passenger demand, we proposed an optimization model for train connections at transfer stations in urban rail transit networks, so that benign interactions between the train flow and passenger flow can be established. In addition, a genetic algorithm was designed to solve the model. Finally, an actual rail network was used as an example to verify the effectiveness of the model and the algorithm. The proposed method can provide theoretical support and practical guidance for the optimized preparation of train schedules (timetables) in urban rail transit networks. This helps solve the existing problem of lack of coordination in the current preparation of train schedules, and promotes the formation of a good cooperative relationship between different lines in terms of passenger transfers within the rail network. In the future studies, we will include the consideration of train delays in order to improve the reliability of train connection optimization results.

CONFLICT OF INTEREST

The authors confirm that this article content has no conflict of interest.

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REFERENCES
