Rapid Measurement of Pseudocontact Shifts in Paramagnetic Proteins by GFT NMR Spectroscopy

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Abstract: Pseudocontact shifts (PCSs) provide valuable structural and dynamic information in (large) proteins. We propose a methodology based on the principle of G-matrix Fourier transform (GFT) NMR spectroscopy for simultaneous and rapid measurement of a large number of PCSs in proteins with a paramagnetic centre. Four experiments, namely, (3,2)D HNNO, (3,2)D HNN(CO)CA, (3,2)D HNN(CO)CA and (3,2)D HNHA taken together facilitate accurate measurement of six PCSs corresponding to ¹H, ¹H, ¹³C, ¹³C', ¹⁵N and ¹⁵N nuclei. In addition, a new algorithm is presented for unambiguous sequence specific resonance assignments of peaks shifted due to PCS. This avoids the need to record multiple 3D correlation experiments. The utility of the proposed experiments is demonstrated with an 8.5 kDa protein, Calbindin. This provides new avenues to a wide range of applications in structure determination/refinement/verification and dynamical studies of proteins in general and paramagnetic proteins in particular.

INTRODUCTION

In recent years, pseudocontact shifts (PCSs) have emerged as one of the most important NMR parameters in calculation, refinement and validation of high-resolution three-dimensional (3D) structures of proteins in solution [1]. These PCSs provide long-range distance information between various NMR active nuclei and the paramagnetic ion as far apart as 45 Å in 3D space [2]. Such information is complimentary to the widely used distance constraints derived from ¹H-¹H NOEs and hence serves to enhance the quality of the resulting structures [3].

PCSs originate due to the presence of a paramagnetic metal centre in a protein possessing anisotropy in its electronic g-factor [4]. A strong anisotropic dipolar interaction between the NMR active nucleus and the unpaired electron gives rise to large changes in chemical shifts of nuclei located within a specific distance of the metal-ion [4]. From the knowledge of the 3D structure of the protein, nature of the metal ion and the assignments available under diamagnetic conditions, the PCS shifted peaks are assigned and corresponding PCSs are measured [5]. These PCSs, in turn, are used for further refinement of the 3D structure [2]. In many instances, spectral overlap due to line-broadening or/and increase in the number of peaks can result in ambiguities for assignments of residues that are pseudocontact shifted. In such cases, a suite of 3D triple-resonance experiments are recorded to aid in their assignment [1, 5b]. While degeneracy in chemical shifts and the spectral overlap can be reduced using 3D NMR experiments, their utility for rapid resonance assignment and structure determination is hampered by long ‘minimal’ measurement time required to acquire data with high digital resolution [6]. Further, this becomes critical if the protein under study is unstable or when the individual PCSs have to be measured with several different metal-ions. This necessitates the development of methods to speed up the process of data collection. In this back drop, we propose a novel methodology that uses a suite of NMR experiments based on the principle of G-matrix Fourier transform (GFT) NMR spectroscopy to rapidly collect the data and analyze and quantify individual PCSs of different nuclei. All the proposed experiments can be acquired in a few hours time and facilitate unambiguous and accurate assignment of PCSs.

GFT NMR spectroscopy [6] is based on phase sensitive joint sampling of two or more chemical shifts in a single dimension, thereby providing higher dimensional spectral information rapidly with high precision. In recent years, GFT NMR has found several applications in resonance assignments and structure determination of biomolecules [6]. Here we describe the concerted use of four GFT NMR experiments namely, (3,2)D HNNO, (3,2)D HNN(CO)CA, (3,2)D HNN(CO)CA and (3,2)D HNHA [6c] facilitating the measurement of PCS of ¹H, ¹H, ¹³C, ¹³C', ¹⁵N and ¹⁵N nuclei. In these experiments, the chemical shifts are jointly sampled for the nuclei shown underlined [6]. Phase sensitive joint sampling of chemical shifts for the two different nuclei is achieved by co-incrementing their respective chemical shift evolution periods wherein one of the shifts is scaled by a factor ‘κ’ relative to the other [6d,e]. After the G-matrix transformation, it results in two sub-spectra each comprising of peaks at a given linear combination of chemical shifts along the indirect dimension: ωᵢ (¹⁵N,i)±κ*Ω(¹³C',i) in (3,2)D HNNO, ωᵢ (¹⁵N,i)±κ*Ω(¹³C',i) in (3,2)D HNN(CO)CA, ωᵢ (¹⁵N,i)±κ*Ω(¹³C',i) in (3,2)D HNN(CO)CA and ωᵢ (¹⁵N,i)±κ*Ω(¹⁵N,i) in (3,2)D HNHA. The scaling factor, κ, allows one to increase the dispersion of peaks or to restrict the chemical shift evolution to avoid losses in sensitivity due to transverse relaxation [6, 7]. A 2D [¹⁵N, ¹H] HSQC provides central peak information (ωᵢ;Ω(¹⁵N)) for all the spectra [6-7].
The experiments are demonstrated with an 8.5 kDa protein called Calbindin that has two Ca\textsuperscript{2+}-binding sites [8]. A paramagnetic lanthanide ion (Yb\textsuperscript{3+}) is introduced in the protein by selective displacement of one of the two metal ions. PCSs are then determined by measuring the difference in chemical shifts observed in the presence and absence of the paramagnetic metal ion.

**METODOLOGY**

**Sample Preparation and NMR Spectroscopy**

Two uniformly \(^{13}\)C and \(^{15}\)N doubly labeled calbindin samples, one with Ca\textsuperscript{2+}-bound to both N- and C-terminal sites ([Ca\textsuperscript{2+}][Yb\textsuperscript{3+}]) and the other Yb\textsuperscript{3+}-substituted in the C-terminal site ([Ca\textsuperscript{2+}][Yb\textsuperscript{3+}]) were purchased from ProtEra SRL (http://www.protera.it). Yb\textsuperscript{3+} was chosen as the paramagnetic metal ion due to its favorable PCS/line-broadening ratio compared to other Ln\textsuperscript{3+} [2a, 5]. The powder sample was dissolved in a mixed solvent of 90% H\textsubscript{2}O/10% \(^2\)H\textsubscript{2}O (pH 6.0) up to a concentration of \(~1.5\) mM. The radio protein called Calbindin that has two Ca\textsuperscript{2+}-binding sites [8]. The experiments are demonstrated with an 8.5 kDa protein [22].

**Table 1. Acquisition Parameters of GFT NMR Experiments**

<table>
<thead>
<tr>
<th>SrNo</th>
<th>Experiment\textsuperscript{a}</th>
<th>Sample</th>
<th>Indirect dimension: (t_{\text{max}}) (ms); Complex points; Digital Resolution (Hz/Pt)\textsuperscript{b}</th>
<th>Meas. time (hrs)</th>
<th>((S/N)^{c})</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>(3,2)D HNCO</td>
<td>[Ca\textsuperscript{2+}]:Cb</td>
<td>(\omega_i(^{15}\text{N}; ^{13}\text{C}): 23.0(^{15}\text{N})/46.0 (^{13}\text{C}); 74; 12.2)</td>
<td>0.3</td>
<td>34.9±6.7</td>
</tr>
<tr>
<td></td>
<td></td>
<td>[Ca\textsuperscript{2+}][Yb\textsuperscript{3+}]:Cb</td>
<td>(\omega_i(^{15}\text{N}; ^{13}\text{C}): 23.0(^{15}\text{N})/46.0 (^{13}\text{C}); 74; 12.2)</td>
<td>0.6</td>
<td>20.5±7.1</td>
</tr>
<tr>
<td>2</td>
<td>(3,2)D HNN(CO)CA</td>
<td>[Ca\textsuperscript{2+}]:Cb</td>
<td>(\omega_i(^{15}\text{N}; ^{13}\text{C}); 22.0(^{15}\text{N})/11.0 (^{13}\text{C}); 52; 12.2)</td>
<td>0.2</td>
<td>14.3±2.8</td>
</tr>
<tr>
<td></td>
<td></td>
<td>[Ca\textsuperscript{2+}][Yb\textsuperscript{3+}]:Cb</td>
<td>(\omega_i(^{15}\text{N}; ^{13}\text{C}); 22.0(^{15}\text{N})/11.0 (^{13}\text{C}); 52; 12.2)</td>
<td>0.4</td>
<td>11.3±3.0</td>
</tr>
<tr>
<td>3</td>
<td>(3,2)D HNN(COCA)CB</td>
<td>[Ca\textsuperscript{2+}]:Cb</td>
<td>(\omega_i(^{15}\text{N}; ^{13}\text{C}); 20.0(^{15}\text{N})/10 (^{13}\text{C}); 128; 11.7)</td>
<td>0.6</td>
<td>28.3±5.3\textsuperscript{d}</td>
</tr>
<tr>
<td></td>
<td></td>
<td>[Ca\textsuperscript{2+}][Yb\textsuperscript{3+}]:Cb</td>
<td>(\omega_i(^{15}\text{N}; ^{13}\text{C}); 20.0(^{15}\text{N})/11.5 (^{13}\text{C}); 128; 11.7)</td>
<td>0.7</td>
<td>13.2±3.3\textsuperscript{d}</td>
</tr>
<tr>
<td>4</td>
<td>(3,2)D HNHA</td>
<td>[Ca\textsuperscript{2+}]:Cb</td>
<td>(\omega_i(^{15}\text{N}; ^{13}\text{C}); 39.0(^{15}\text{N})/18 (^{13}\text{C}); 180; 8.0)</td>
<td>1.5</td>
<td>32.1±3.2</td>
</tr>
<tr>
<td></td>
<td></td>
<td>[Ca\textsuperscript{2+}][Yb\textsuperscript{3+}]:Cb</td>
<td>(\omega_i(^{15}\text{N}; ^{13}\text{C}); 39.0(^{15}\text{N})/18 (^{13}\text{C}); 180; 8.0)</td>
<td>3.0</td>
<td>28.1±3.6</td>
</tr>
</tbody>
</table>

\textsuperscript{a} A 2D \(^{15}\text{N}; ^{1}\text{H}\) HSQC was recorded as central peak spectra for calbindin without Yb (~5 minutes) and with Yb (~10 minutes).

\textsuperscript{b} Direct dimension \(\omega_i(\text{H})/\omega_i(\text{H})\); 75; 812; 10.0.

\textsuperscript{c} S/N is calculated as ratio of the peak height to 2.5*standard deviation of the noise.

\textsuperscript{d} With cryogenic probe on 600 MHz.
the (3,2)D GFT spectra was facilitated using the central peak information \((15N)\) obtained from the 2D \([15N, 1H]\) HSQC (Fig. S4). The PCS shifted peaks observed in GFT spectra of \([Ca^{2+}][Yb^{3+}]Cb\) were then assigned to their parent peaks in \([Ca^{2+}]Cb\) as follows. First a list of \(1^H N\), \(1^H\), \(1^H^{13} C\) and \(1^H\) chemical shifts were compiled for each spin system of \([Ca^{2+}]Cb\) (hereby denoted as \(list\ A\)) and \([Ca^{2+}][Yb^{3+}]Cb\) (hereby denoted as \(list\ B\)). The set of six chemical shifts then uniquely identifies a residue, as it is impossible for any two amino acid residues in a given protein to have all the six chemical shifts degenerate (Fig. S5).

In the next step, the chemical shift list obtained for the \([Ca^{2+}]Cb\) (\(list\ A\)) was compared with that of the \([Ca^{2+}][Yb^{3+}]Cb\) (\(list\ B\)). For each set \(i\) in \(list\ A\), containing six chemical shift values, a root mean square deviation (r.m.s.d.) was calculated with each set of shifts, \(j\), in \(list\ B\) as:

\[
\text{r.m.s.d.}(i, j) = \sqrt{\frac{\sum (X_{list\ A} - X_{list\ B})^2}{n}}
\]

where (i) \(X_{list\ A/list\ B} = (1^HN), (1H), (13C), (13C), (13C'), and (15N)\), (ii) \(n\) denotes the number of shift types (i.e., \(X_{list\ A/list\ B}\) being included in the calculation for a given spin system and (iii) \(i, j\) denote the entry number of the set in \(list\ A\) and \(list\ B\), respectively. The set \(j\) in \(list\ B\) having the least r.m.s.d. with a given set \(i\) in \(list\ A\) was taken as the PCS shifted set of shifts for \([Ca^{2+}][Yb^{3+}]Cb\) corresponding to its respective non-shifted set of chemical shifts measured in \([Ca^{2+}]Cb\). Note that this is equivalent to calculating the distance between two signals in the six-dimensional chemical shift space comprising the six chemical shifts being measured.

**RESULTS AND DISCUSSION**

Fig. (1) shows an overlay of 2D \([15N-1H]\) HSQC spectra acquired with \([Ca^{2+}]Cb\) (peaks shown in blue) and \([Ca^{2+}][Yb^{3+}]Cb\) (peaks shown in red). For illustrative purpose, peaks in \([Ca^{2+}]Cb\) spectrum exhibiting \(1^HN\) and \(15N\) PCS of more than 0.5 ppm are shown connected to their respective peaks in \([Ca^{2+}][Yb^{3+}]Cb\) spectrum with dotted arrows.

![Overlay of 2D [15N-1H] HSQC spectra acquired with [Ca^{2+}]Cb and [Ca^{2+}][Yb^{3+}]Cb](image)

The PCS shifted peaks in 2D \([15N, 1H]\) HSQC corresponding to Fig. (1) was facilitated using the central peak information \((15N)\) obtained from the 2D \([15N, 1H]\) HSQC (Fig. S4). The PCS shifted peaks observed in GFT spectra of \([Ca^{2+}][Yb^{3+}]Cb\) were then assigned to their parent peaks in \([Ca^{2+}]Cb\) as follows. First a list of \(1^HN\), \(1^H\), \(1^H^{13} C\) and \(1^H\) chemical shifts were compiled for each spin system of \([Ca^{2+}]Cb\) (hereby denoted as \(list\ A\)) and \([Ca^{2+}][Yb^{3+}]Cb\) (hereby denoted as \(list\ B\)). The set of six chemical shifts then uniquely identifies a residue, as it is impossible for any two amino acid residues in a given protein to have all the six chemical shifts degenerate (Fig. S5).

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\[
\text{r.m.s.d.}(i, j) = \sqrt{\frac{\sum (X_{list\ A} - X_{list\ B})^2}{n}}
\]

where (i) \(X_{list\ A/list\ B} = (1^HN), (1H), (13C), (13C), (13C'), and (15N)\), (ii) \(n\) denotes the number of shift types (i.e., \(X_{list\ A/list\ B}\) being included in the calculation for a given spin system and (iii) \(i, j\) denote the entry number of the set in \(list\ A\) and \(list\ B\), respectively. The set \(j\) in \(list\ B\) having the least r.m.s.d. with a given set \(i\) in \(list\ A\) was taken as the PCS shifted set of shifts for \([Ca^{2+}][Yb^{3+}]Cb\) corresponding to its respective non-shifted set of chemical shifts measured in \([Ca^{2+}]Cb\). Note that this is equivalent to calculating the distance between two signals in the six-dimensional chemical shift space comprising the six chemical shifts being measured.

**RESULTS AND DISCUSSION**

Fig. (1) shows an overlay of 2D \([15N, 1H]\) HSQC spectra acquired with \([Ca^{2+}]Cb\) and \([Ca^{2+}][Yb^{3+}]Cb\) samples. The PCS shifted peaks in 2D \([15N, 1H]\) HSQC corresponding to

![Overlay of (3,2)D GFT spectra recorded with ([Ca^{2+}]Cb) and ([Ca^{2+}][Yb^{3+}]Cb). The respective linear combination of chemical shifts that are observed in each GFT sub-spectra is indicated in each panel. In the case of (3,2)D HNNCO, (3,2)D HNN(CO)CA and (3,2)D HNN(COCA)CB, peaks shown in blue correspond to ([Ca^{2+}]Cb) and those in red correspond to ([Ca^{2+}][Yb^{3+}]Cb). In (3,2)D HNHA, peaks comprising \(\omega_1\); (\(15N\)±\(k\)\(\omega_1\)(\(1H\)) chemical shifts are shown in blue and green for ([Ca^{2+}]Cb) and ([Ca^{2+}][Yb^{3+}]Cb), respectively, and peaks comprising \(\omega_1\); (\(15N\)±\(k\)\(\omega_1\)(\(1H\)) chemical shifts are shown in pink and black for ([Ca^{2+}]Cb) and ([Ca^{2+}][Yb^{3+}]Cb), respectively.](image)
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[Ca$^{2+}$][Yb$^{3+}$]Cb (shown in red; Fig. 1) were assigned to their non-shifted parent peaks corresponding to [Ca$^{2+}$]Cb (shown in blue) using the algorithm described above. The generally observed fact that both $^{15}$N and $^1$H$^N$ nuclei in a given amino acid residue exhibit up-field or down-field PCS [5] served to verify these assignments.

In 2D [$^{15}$N, $^1$H] HSQC of [Ca$^{2+}$][Yb$^{3+}$]Cb and the different GFT spectra, peaks were not observed for ~30% of residues. On inspection of the 3D structure, the amide moieties of these residues (18-26, 52-66) were found to be located within a radius of 6.9 ± 2.7 Å from Yb$^{3+}$ (Fig. S6) leading to loss of signal due to extensive line broadening [2a]. A total of 104 $^1$H$^N$ and $^{15}$N PCS were measured which is similar to the number of PCS measured in the earlier studies [2a].

Fig. (2) shows the four GFT (3,2)D spectra recorded on the two samples. The respective acquisition parameters and sensitivity are given in Table 1. Fig. (3) shows the measured PCS as a function of residue number for different nuclei obtained using the methodology described above. The GFT spectra acquired with ([Ca$^{2+}$][Yb$^{3+}$]Cb yield a lower number of PCSs compared to that obtained from 2D [$^{15}$N, $^1$H] HSQC (Fig. 2, 3). This is due to the fact that the various GFT experiments employ additional delay periods for polarization transfer to various nuclei ($^{13}$C, $^{13}$C', $^{13}$C, $^1$H), which have stronger dipolar interaction with the paramagnetic centre and hence have reduced sensitivity for residues close to the metal ion. Fig. (4) depicts the magnitude and the sign of PCS measured for different nuclei mapped onto the high-resolution 3D structure of lanthanide substituted Calbindin [3]. Peaks corresponding to residues 18-26 and 52-66 come close in space to the paramagnetic metal ion Yb$^{3+}$ (Fig. S6) and hence are not observed in many of the spectra due to severe line broadening [2a]. For other residues, the magnitude of PCS decreases with increase in the distance from the metal ion in accordance with theory.

One of the challenging tasks in structural studies of proteins containing paramagnetic metal ions is the sequence specific assignment of PCS shifted peaks [15]. This is typically accomplished using a set of 3D triple resonance experiments that are used for sequential resonance assignment of diamagnetic proteins [16]. In the present study, complete unambiguous assignments were obtained using the novel algorithm described above without recourse to any sequential assignment procedure. This methodology uses the chemical shifts of $^1$H, $^{13}$C, $^{15}$N and $^1$H$^N$ in conjunction with those of $^{15}$N and $^1$H$^N$. The underlying assumption of the algorithm is that PCS acts as a perturbation of diamagnetic chemical shift values and therefore a given residue is expected to remain in its vicinity (quantified by r.m.s.d.) in the six-dimensional chemical shift space comprising the six chemical shifts being measured. Thus, in the presence of a paramagnetic metal ion, any spin undergoing PCS can be unambiguously traced back to its source (original) peak in the diamagnetic protein by measuring different types of chemical shifts and using the methodology described above (Eqn. [1]). The utility of the algorithm was tested using the data acquired on Calbindin by successively including various chemical shifts in Eqn. [1]. It is observed (Fig. S5) that using only $^{15}$N and $^1$H chemical shifts, 8 residues in Calbindin undergoing PCS have lower r.m.s.d. to residues other than their own in the diamagnetic state. Thus, use of information about

Fig. (3). Plot of the different PCSs measured using (3,2)D GFT spectra as a function of amino acid residues of calbindin. The $^1$H, $^{13}$C and $^{15}$N resonance assignments obtained for [Ca$^{2+}$][Yb$^{3+}$]Cb sample has been deposited in the BMRB under accession code 15594.
two residues with a different set of six chemical shifts (i.e. well separated in 6D chemical shift space) in the diamagnetic protein to overlap in the six-dimensional chemical shift space upon addition of the paramagnetic metal-ion (verified using a chemical shift database of 235 proteins obtained from BioMagResBank (http://www.bmrb.wisc.edu); Fig. S5). Notably, this algorithm can be applied to any set of higher dimensional chemical shift correlation data recorded for the assignment of PCS shifted peaks and are not limited to the chosen set of GFT experiments described here. In case of residues in close vicinity of the metal-ion, severe line-broadening leads to absence of peaks. The extent of line-broadening and hence the sensitivity of the experiments will depend on the choice of Ln³⁺ [2a]. Thus for a given residue, if the chemical shifts of specific nuclei are not measured, the r.m.s.d. (Eqn [1]) is calculated using the available chemical shifts for that residue.

The accuracy of the PCS values measured with the GFT spectra was evaluated by comparison with (i) PCS measured using conventional triple resonance 3D NMR experiments (Fig. 5A; for comparison of ¹⁵N and ¹H⁶ pcs, the values given in Ref. 2a was used) and ii) PCS predicted with FANTASIAN [13] (Fig. 5B) using the high-resolution 3D structure of Calbindin (1ksm.pdb; Fig. 4) as the reference. Since systematic errors are negligible for GFT NMR-based measurement of PCS (Fig. 5), one can compare the precision of measurements for each type of PCS by considering that r.m.s.d. = sqrt[(σ²(GFT) + σ²(conventional)] when σ denotes the error/standard deviation of PCS measured. Assuming both GFT and its 3D congener have similar errors in PCS, r.m.s.d = σ*√2. Based on this, a precision (σ) of 0.03-0.2 ppm is obtained for the measurement of different PCS. Measuring the PCS with high precision and accuracy renders them useful for 3D structure refinement protocols employing PCS [17] where the accuracy of the structure depends critically on the accuracy of the calculated alignment tensor.

**CONCLUSIONS**

We propose a novel methodology based on the principle of GFT NMR spectroscopy for rapid and accurate measurement of six different PCSs in paramagnetic proteins. The concerted use of the six different PCSs helps in accurate prediction of molecular alignment tensor for 3D structure refinement. The measurement times can be reduced further in combination with other fast data collection methods, such as longitudinal ¹H relaxation optimization [6b]. In the case of large proteins, the experiments presented here can be combined with deuteration [18] and TROSY [19] for increased resolution/sensitivity. Taken together, these experiments will have wide range of applications in structure determination and refinement of proteins in general and paramagnetic proteins in particular.
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REFERENCES


SUPPORTING INFORMATION FOR:
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Figure S1. R.f. pulse scheme of GFT (3,2)D HNNCO. Rectangular 90° and 180° pulses are indicated by thin and thick vertical bars, respectively, and phases are indicated above the pulses. Where no r.f. phase is marked, the pulse is applied along x. High-power 90° pulse lengths are: 10.0 μs for 1H, 35 μs for 15N and 14.8 μs for 13C. κ=0.5 (see text). The 1H r.f. carrier is placed at the position of the solvent line at 4.7 ppm. The 15N carrier position is set to 121.0 ppm. The 13C' carrier is placed at 176 ppm. A Gaussian shaped 1H r.f. pulse [1] of length 1.0 ms is used for water flip-back prior to the first r.f. pulse on 15N. DIPS-2 [2] is used for 1H decoupling during heteronuclear coherence transfer periods. GARP [3] is employed to decouple 15N (r.f.=1.50 kHz) during acquisition. All pulsed z-field gradients (PFGs) are sine-bell shaped shaped with gradient recovery delay of 200 μs. The duration and strengths of the PFGs are: G1 (0.5 ms, 30 G/cm); G2 (0.5 ms, 20 G/cm); G3 (1.0 ms, 10 G/cm); G4 (2.0 ms, 40 G/cm); G5 (1.0 ms, 4 G/cm). The delays are: \( t_1 = 2.3 \) ms, \( t_2 = 5.5 \) ms, \( e=100\mu s \) and \( t_3 = 12 \) ms. Phase cycling: \( \phi_1 = x, -x; \phi_2 = 2(x), 2(-x); \phi_3 = 2(y), 2(-y); \phi(\text{receiver}) = x, -x, -x, x \). A sensitivity enhancement scheme [4] is employed, i.e., the sign of G2 is inverted in concert with a 180° shift of \( \phi_1 \). GFT NMR phase-cycle: \( \phi_1 = x, y \) yields, in conjunction with quadrature detection in \( t_1(15N) \), 2 data sets which are linearly combined employing a G-matrix transformation with the G-matrix [5-6].
Figure S2. R.f. pulse scheme of GFT (3,2)D HNN(CO)CA. Rectangular 90° and 180° pulses are indicated by thin and thick vertical bars, respectively, and phases are indicated above the pulses. Where no r.f. phase is marked, the pulse is applied along x. High-power 90° pulse lengths are: 10.0 μs for 1H, 35 μs for 15N and 14.8 μs for 13C, 3=0.5 (see text). The 1H r.f. carrier is placed at the position of the solvent line at 4.7 ppm. The 15N carrier position is set to 121.0 ppm. The 13C' carrier is placed at 176 ppm before the first pulse on 13C and shifted back to 176 ppm after the last 90° r.f. pulse on 13C. A Gaussian shaped 1H r.f. pulse [1] of length 1.0 ms is used for water flip-back prior to the first r.f. pulse on 15N. DIPSI-2 [2] is used for 1H decoupling during heteronuclear transfer periods. GARP [3] is employed to decouple 15N (r.f.=1.50 kHz) during acquisition. All pulsed z-field gradients (PFGs) are sine-bell shaped shaped with gradient recovery delay of 200 μs. The duration and strengths of the PFGs are: G1 (0.5 ms, 30 G/cm); G2 (2.0 ms, 40 G/cm); G3 (2.0 ms, 4 G/cm). The delays are: τ1 = 2.3 ms, τ2 = 5.5 ms, τ3 = 12.5 ms, τ4 = 4.0 ms. Phase cycling: φ1 = x; φ2 = 2(x),2(-x); φ3 = 2(y),2(-y); φ(receiver) = x, -x, -x, x. A sensitivity enhancement scheme [4] is employed, i.e., the sign of G2 is inverted in concert with a 180° shift of φ3. GFT NMR phase-cycle: φ1 = x, y yields, in conjunction with quadrature detection in t1(15N), 2 data sets which are linearly combined employing a G-matrix transformation with the G-matrix [5-6].
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Figure S3. R.f. pulse scheme of GFT \((3,2)D\) HNN(COCA)CB. Rectangular 90° and 180° pulses are indicated by thin and thick vertical bars, respectively, and phases are indicated above the pulses. Where no r.f. phase is marked, the pulse is applied along \(x\). High-power 90° pulse lengths are: 10.0 \(\mu\)s for \(^1H\), 35 \(\mu\)s for \(^{15}N\) and 14.8 \(\mu\)s for \(^{13}C\). \(\kappa=0.5\) (see text). The \(^1H\) r.f. carrier is placed at the position of the solvent line at 4.7 ppm. A Gaussian shaped \(^1H\) r.f. pulse [1] of length 1.0 ms is used for water flip-back prior to the first r.f. pulse on \(^{15}N\). The \(^{15}N\) carrier position is set to 121.0 ppm. The \(^{13}C'\) carrier is placed at 176 ppm and switched to 56 ppm before the first r.f. pulse on \(^{13}C''\) and switched back to 176 ppm after the last r.f. pulse on \(^{13}C'\). A six-pulse composite sequence [7] is used to simultaneously invert/refocus \(^{13}C''/^{13}C'\) magnetization during \(^{13}C''/^{13}C'\) polarization transfer.

The 90° and 180° pulse lengths of \(^{13}C''\) are adjusted (at a \(^1H\) resonance frequency of 600 MHz) to 54 \(\mu\)s and 46 \(\mu\)s, respectively, to minimize perturbation of the \(^{13}C'\) spins. DIPSI-2 [2] is used for \(^1H\) decoupling during heteronuclear transfer periods. GARP [3] is employed to decouple \(^{15}N\) (r.f. = 1.50 kHz) during acquisition. All pulsed z-field gradients (PFGs) are rectangular shaped. The duration and strengths of the PFGs are: G1 (0.5 ms, 10 G/cm); G2 (0.5 ms, 10 G/cm); G3 (1.0 ms, 20 G/cm); G4 (0.5 ms, 10 G/cm); G5 (0.5 ms, 10 G/cm); G6 (1.25 ms, 22 G/cm); G7 (0.5 ms, 10 G/cm); G8 (0.125 ms, 22 G/cm). The delays are: \(\tau_1=2.3\) ms, \(\tau_2=5.5\) ms, \(\tau_3=100\mu\)s, \(\tau_4=12.5\) ms, \(\tau_5=4.0\) ms; \(\tau_6=7.2\) ms. Phase cycling: \(\phi_1=x, -x; \phi_2=y, -y; \phi_3=2(x), 2(-x); \phi_{(receiver)}=x, -x, -x, x\). A sensitivity enhancement scheme [4] is employed, i.e., the sign of G6 is inverted in concert with a 180° shift of \(\phi_4\). GFT NMR phase-cycle: \(\phi_1=x, y; \phi_2=y, -x\) yields, in conjunction with quadrature detection in \(t_i(15N)\), 2 data sets which are linearly combined employing a G-matrix transformation with the G-matrix [5-6].
Figure S4: A screen capture using the software XEASY illustrating the identification/assignment of a pair of peaks belonging to an amino acid residue in (3,2)D GFT sub-spectra (shown in (a), (b)) along the indirect dimension: \( \omega_i: \Omega(\text{^{15}N}) \pm k^* \Omega(X) \) (\( X=^1\text{H}^N, ^1\text{H}^H, ^{13}\text{C}^\alpha, ^{13}\text{C}^\beta, ^{13}\text{C}' \) and \( ^{15}\text{N} \)) using the central peak information (\( \omega_i: \Omega(\text{^{15}N}) \)) obtained from the 2D [\( ^{15}\text{N}, ^1\text{H} \)] HSQC spectrum (shown in (c)). The particular spectrum shown corresponds to (3,2)D GFT HNNCO. The linear combination of the chemical shifts observed is indicated on the top. The symmetrical distribution of the peaks in GFT sub-spectra encoding the two linear combination of chemical shifts about the central peak (\( \omega_i: \Omega(\text{^{15}N}) \)) facilitates the identification/assignment. In the event of two or more amino acids having degenerate \( ^1\text{H}^N / ^{15}\text{N} \) chemical shifts, the methodology described in Ref. 7d (in main text) is adopted.
Figure S5:

(A) Estimation of percentage of residues in proteins having degenerate chemical shifts. The estimation was carried out using a database of 235 proteins with known chemical shift assignments downloaded from the BioMagResBank (http://www.bmrb.wisc.edu). The percentage degeneracy was calculated by counting the number of residues that have degenerate chemical shifts with t spins belonging to other residues in any protein within a given tolerance limit (which was chosen as 0.3 ppm for all nuclei corresponding to the average PCS observed in Calbindin). Thus, about 30-40% of residues in a given protein can have degenerate $^1$H and $^{15}$N chemical shifts within this tolerance limit. However, the percentage degeneracy decreases as additional chemical shifts ($^1$H, $^{13}$C, $^{13}$C, $^{15}$C') are included in the calculation. Thus, the chemical shift information of the chosen set of six spins uniquely identifies an amino acid residue. This implies that no two amino acid residues in a given protein will have all the six chemical shifts degenerate.

(B) Number of amino acid residues having non-zero PCSs in Yb$^{3+}$ substituted Calbindin that have a lower r.m.s.d. (calculated using Eqn. [1]; See main text) to the residues other than their own in the diamagnetic state. As is evident, use of information about the $^1$H and $^{15}$N chemical shifts alone renders their assignment ambiguous. It would then require information from 3D NMR experiments used for sequential resonance assignments to arrive at residue specific assignment. On the other hand, this number of residues that have lower r.m.s.d decreases on inclusion of additional chemical shifts ($^1$H, $^{13}$C, $^{13}$C, $^{15}$C') in Eqn. [1] and thus aid in their rapid assignment. This implies that the pair comprising the PCSs and the corresponding diamagnetic counter-part gets uniquely identified by their lowest r.m.s.d. compared to that of all other possible pairs of residues when 4 or more different chemical shifts are included.
Figure S6: Residues for which PCS were not observed in both conventional 3D NMR experiments and their GFT-NMR counter parts of [Ca$^{2+}$$][Yb^{3+}]$Cb sample (1ksm.pdb) are depicted in red color. The cyan color represents the paramagnetic ion ($Yb^{3+}$). The residues from 18-26 and 52-66 regions show higher broadening in the case of $Yb^{3+}$. The amide moieties of these residues were found to be located within a radius of $6.9 \pm 2.7 \, \text{Å}$ from $Yb^{3+}$.

REFERENCES