On Cancer Cell Cycle and Universal Apoptosis Parameters Signaling Unravelled In Silico

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Abstract: Here, cell cycle in higher eukaryotes and their molecular networks signals both in G1/S and G2/M transitions are in silico replicated. Systems control theory is employed to design multi-nestled digital layers to simulate protein-to-protein activation and inhibition in the cancer cell cycle dynamics in presence of damaged genome. Sequencing and controlling the digital process of four micro-scale species networks (p53/Mdm2/DNA damage; p21mRNA/cyclin-CDK complex; CDK/CDC25/wee1/SKP2/APC/CKI and apoptosis target genes system) paved the way for unravelling the participants and their by-products having the task to execute (or not) cell death. The results of the proposed cell digital multi-layers give reason to believe in the existence of an universal apoptotic mechanism. We identified and selected cell checkpoints, sizers, timers and specific target genes dynamics both for influencing mitotic process and avoiding cancer proliferation as much as for leading the cancer cell(s) to collapse into a steady stable apoptosis phase.

Keywords: Cell signalling, cell digital simulator, cancer cells, apoptosis.

INTRODUCTION

Both in higher eukaryotes and yeast, the duty cycle period between two successive divisions depends on cell size which can be divided into two sub-phases, one called sizer and timer the other one [1-5].

New approaches as mathematical modeling, non linear system dynamics and digital signal analysis are even more employed for deeper insights into cellular biological process [6-17].

Mathematical bifurcation analysis meets with outstanding success for modeling biochemical reactors and regulators of eukaryotes cell cycle in terms of molecular antagonism, hysteresis, irreversible transition up to intrinsic pathway of programmed cell death [18-22].

As regards cell growth, Tyson and colleagues [15-17,23-25] suggest elegantly saddle-node bifurcation for the G1/S transition checkpoint and saddle-node-loop bifurcation for the G2/M phase checkpoint, so as to resume cell activities into a bistable system. However, other important features, such as sizers and timers remain to be explained.

Diametrically opposite opinions lead other authors [1,2,18] to mathematically model cell cycle using Hopf bifurcation analysis in which sizers and timers arise naturally as features of cell signaling network.

Here, cell growth protein-to-protein signaling networks and their co-factors and by-products, see Fig. (1), are firstly translated into mathematical frames and then linked to each other via multi-nestled digital layers, sub-blocks and control wirings, see Figs. (2-5).

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Fig. (1). Wiring diagram of the molecular model of cancer cell species dynamics.

Fig. (2). Human cell DNA damage-repair master digital simulator (overall view).
Fig. (3). Digital sub-networks of p21mRNA/p21 and apoptotic target genes.

Fig. (4). Sub-layer of the cell sizers, timers and checkpoints network.
Fig. (5). Digital sub-network of cell cycle activities (division, cell fate, growth and growth arrest).

genes system, i.e., cyclin-dependent kinase CDK/CDC25/ inhibitor, p21; p53-regulated apoptosis-inducing protein 1, p53AIP1; apoptotic protease activating factor 1, APAF1; and target gene "cytoc" as a functional of APAF1 in apoptosome expression being its value, expressed by the Heaviside function, equal to 1 (or zero) for matching (or not) the cell death.

Biochemical and Digital Sub-Layer of p53/Mdm2/DNA Network

In cell cycle of cancer pathologies, the oncosuppressor p53 protein induces the transcription of genes in charge of the cell-cycle arrest, DNA repair and apoptosis [28-40].

In a human cell, the biological response of ATM, p53 and Mdm2 species is interlinked with, and quite similar to, the output response of oscillating network dynamics. If DNA damage exceeds a threshold, the p53 pulses to activate transcription of the p21 gene and other species for apoptosis execution [41-56].

We start by taking into account the protein forms of p53 (p53 mono-ubiquitinated, p53 poly-ubiquitinated and p53 total, i.e., p53U, p53U and p53tot, respectively) and Mdm2 (nuclear, cytoplasmic and phosphorylated, i.e., Mdm2nuc, Mdm2cyt and Mdm2phs, respectively) with their time-dependency from a set of equations. From a biotechnological point of view, the problem consists of processing a set of equations in a computational space, i.e., the state space which mathematically represents all the possible conditions and combinations of the variables of the problem. Here, the biological basis upon which the present p53/Mdm2/DNA damage digital model are those of Ciliberto et al. [30]. In the present simulations, a generic variable (DNA damage) DNA_{dam} depends upon IR (Ionizing Radiation). The mathematical translations and the corresponding digital sub-block features are obtained as displayed in Fig. (2). Both p53/Mdm2 positive/negative feedback loops are generated and processed via the control matrices BB and K which are located between the Mdm2 and p53 proteins dynamic systems for a real-time check of the digital output variables (protein kinases and their time rates).

BB is a matrix block that is employed to build up the control matrix feedback, K, in the LQR (Linear Quadratic Regulator) system; k_d^2 block digitally performs the rate constant for degradation of Mdm2nuc.

Biotechnological processors are applied to the continuous time-linear p53/Mdm2/DNA damage system that can be summarized by:

$$\dot{x} = Ax + Bu \tag{1}$$

where:

$$x$$ is the derivative of state-vector,

$$\dot{x}(t) = P\left([Mdm2_{nu}(t)]\right)x(t) + b \tag{2}$$

is the matrix for p53 transcription factor dynamics, B is the matrix for the transition (LQR) input-state, u is the LQR input.

The feedback control law requires that:

$$u = -Kx \, ; \, K = R^{-1}B^T \tag{3}$$

$$A^T P + PA - PBR^{-1}B^T P + Q = 0 \tag{4}$$

Q is a semi-definite positive matrix containing, as elements, the inverse of the square maximum values of the proteins concentrations R is a definite positive matrix containing, as elements, the inverse of the square maximum
values of the input signals $K$ is the control matrix feedback $P$ is the stabilizing solution of Riccati equation (in matrix terms). The state-vector for p53 and its concentrations shall be

$$\dot{x}(t) = \begin{bmatrix} p^{53} \\ p^{53}_s \\ p^{53}_u \\ p^{53}_i \\ p^{53}_u \\ p^{53}_i \\ p^{53}_u \\ p^{53}_i \\ p^{53}_u \end{bmatrix}$$

(5)

Once the proposed state-space representation gives the same results as the model of Ciliberto et al. [30], the digital optimal control law has been implemented and based on the assumption that the matrix is such that $M_{auc}$ is equal to a constant

In a similar way:

$$\dot{z}(t) = M \begin{bmatrix} p^{53}_a(t) \\ k_{d_1}(t) \end{bmatrix} + C \begin{bmatrix} p^{53}_a(t) \end{bmatrix}$$

(6)

Moreover, some auxiliary matrices have been employed as follows for the LQR shakedown

$$K = LQR \begin{bmatrix} 4, 2, 0, 2 \end{bmatrix}$$

(7)

where

$$P = \begin{bmatrix} P_i; i, j = 1, 2, 3; P_i \in \mathbb{R} \end{bmatrix}$$

(8)

The optimal control matrix has to accomplish the task to accelerate the DNA repair process according to the equation:

$$\frac{d[DNA_{sun}]}{dt} = k_{d_1} + k_{d_2}[DNA_{sun}] - \frac{[DNA_{sun}]}{[DNA_{sun}]}$$

(9)

Biochemical Assumptions and Digital Sub-Layer of p21mRNA/cyclin-CDK Complex

We assume p21mRNA is indirectly connected to DNA damage capable of activating chk1 protein which inhibits CDC25 activity. In agreement with but differently from Qu et al. [1,2], we translate biochemical p21mRNA/cyclin-CDK chain kinase reactions into a differential equation

$$\frac{dx}{dt} = f(z)x - \frac{g(w)x - \delta p21mRNAx}{\delta}$$

(10)

For digitally designing and checking the cell multi-layers, we assume a numerical value for $\delta$ so as to obtain the same starting level of DNA damage of Qu et al. [1]. The digital scheme of p21mRNA/cyclin-CDK complex involves a multi-nested layer. The first (see "p21 Subsystem1" block circuitry and Sub-Block A in Fig. (3)) replicates in silico the protein-to-protein signaling between p21 and all the considered forms of p53 via Goldbeter-Koshland function. A complex digital switching chain (see Sub-Block B of Fig. (3)) injects several combinations of p21mRNA input signal during cell cycle transition phases. Both natural and controlled p21mRNA signalling pathways are generated and further processed by the cell growth dynamics digital multi-layers of Fig. (4).

Biochemical Assumptions and Digital Sub-Layer of CDK/CDC25/wee1/SKP2/APC/CKI Network

Following Qu et al. [1] and the proteins kinase map of Fig. (1), the biochemical synthesis of the considered species has to be translated into differential equations.
Apoptosis" (see Fig. (2)) to p53 forms and cyclin-CDK sub-blocks; also, the p21mRNA digital block (see Fig. (3)) and the sub-layers of "Cell Division Control System", "Cell Cycle Dynamics" and Cell sizers & checkpoint control system" (see Figs. (4-5)) trigger concurrent and dialoguing signaling with apoptosis target genes network.

RESULTS

Cell Cycle Arrest on DNA Damage Target Genes Response

Separately, two square-wave radiation signals were emitted for causing a fixed level of DNA damage and evaluating (if any) sizers, timers and checkpoints variations.

The onset of these two distinct signals is tuned and exerted for 10min both in the G1/S phase (at t=50min) and in G2/M transition phase (at t=1100min), respectively. Pictorial outfits of apoptotic target genes responses to DNA damage impulse at t=50min (see Fig. (6)) reveal double-pulsing features of p21mRNA along the timespan. After a quiescent state, within 200÷250min, p21mRNA starts to rise its level of synthesis according to a first instability in p53AIP1, APAF1 and cytoc pathways; looping in chain, for this time window, p21mRNA underexpression runs in choral way with a low speed degradation rate of APAF1.

Once a second instability of the apoptotic species occurs, 250÷300min, p21mRNA radically changes its pathway and increases with high speed synthesis rate. For the time window 2000÷5000min (digitally, \( t \to \infty \)), p21mRNA expression assumes stable and undamped oscillations and begins to pulse in-phase with active cyclin-CDK frequency (see also Fig. (7)). Conversely, the APAF1 degradation (inverse) gradient increases and its concentration falls during the timespan 200÷300min; past this time window, it remains quiescent.

The digital simulations make almost superimposable the mutual dynamics of these two species, active cyclin-CDK and p21mRNA, regulated with a negative feedback loop with those obtained by bifurcation analysis and confirm the p21mRNA low speed synthesis rate. Instead, cell species signaling networks involve high speed rate of p21mRNA synthesis as a response to damaged genome. Comparison among cell growth regulation species (see Fig. (7)) with undamaged cell cycle [1], show delay in active cyclin-CDK (as well as APC) synthesis causing a variation in the "natural" cell cycle timespan. This cell cycle time window delay being equal to the cell growth time window arrest. Looking at the cell mass and active wee1 dynamics panels (Fig. (7)), after a transient regarding the first two instabilities of p53AIP1, APAF1, cytoc and the first two oscillations of p21mRNA, one has to note that these cell parameters pulse in-phase with APC and active cyclin-CDK complex. Thus, only the cellular timer phase is affected by DNA damage repair while checkpoints and sizers remain steady stable. This causes a constant pulsing frequency phase variation among the cell cycle-dependent species of aberrant cell and those concerning a cell structure in which DNA was repaired. In the second simulation (see Fig. (8)), DNA damage triggers at t=1100min and cell network species show absence of a bistable behavior of active cyclin-CDK in mitotic phase; this implies no modifications in p21mRNA response to DNA damage repair. Within the timespan 1150÷1950min, cell starts division into two daughter cells and the increasing cyclin-CDK complex activity acts for inhibiting p21mRNA overexpression in the mother cell. APC, cell mass and wee1 panels (see Fig. (9)) pictorially display the capability of cell digital multi-layer platform to describe cell(s) checkpoints, timers and sizers. Differently from the previous simulation (DNA damage at t=50min), here cell cycle steps forward the time window 1150÷1950min in which G2/M transition occurs and differences between the two performed simulations become more evident. Strictly speaking, at G2/M, high speed rate activities of cyclin-CDK complex are combined with p21mRNA modified pulsing pathway (lowest peak and highest frequency); when mitotic process (M phase) is accomplished, p21mRNA decreases its frequency (and

![Fig. (6). Output response of apoptotic species network as a consequence of DNA damage at t=50min.](image-url)
highest peak of concentration) in the daughter cells and re-enters a steady state undamped oscillations in-phase with active cyclin-CDK complex, APC and wee1.

As a consequence, the cell growth time arrest is equal to the delay of cell cycle species synthesis and cell checkpoints, timers and sizers behaviors are the same of those evaluated at t=50min.

**p21mRNA "Tracking" Signaling and Apoptosis Network**

Normally, if a DNA damage affects genome integrity during physiological cell cycle, molecular emergence resources system is immediately activated Digitally (and biochemically), this cell defence machinery backwardly and forwardly pulses a signaling "dialogue" towards critical cell cycle reactors and factors conditioning repetitive cycles, checkpoints and size progression. Essentially, the p53/Mdm2 feedback loop system digital behavior consists of zero, one, two or more pulses as a function of DNA damage. Based on previous studies [26,27,30], a key role is played by p21mRNA and its dynamics. If irreversible DNA damage is present, p21mRNA synthesis remains almost quiescent at the beginning of the apoptotic time window but triggers suddenly with a concurrent and specific pathways of apoptotic target genes having as a consequence the closure of the apoptotic time window and allowing the cell to avoid its fate.

This peculiar and malicious mechanism of p21mRNA was previously studied by the first author [27] for identifying its interaction with apoptosis genes. In that previous digital...
approach, the results are in experimental agreement with those of Viale et al. [55]. In that case, p53-independent p21mRNA overexpression showed an unforeseen dynamics when related to the apoptosis genes pathways. When different signals of p21mRNA were triggered, the response of the p53/Mdm2 network radically changed into an impulse train of prolonged undamped oscillations whose amplitude and frequency is one order higher than the case in which the DNA was quickly repaired. Looking (clockwise) at the panels of Fig. (10), we evaluate the apoptosis p21mRNA signal-dependency and demonstrate a sort of "digital-sequenced tracking radome" property of p21mRNA to instantly identify the wavelengths and frequencies of the apoptotic species and intercept their gradient inversions. For this aim, we suppose different signal pathways of p21mRNA over different triggering timespans.

At first, let p21mRNA be represented by a negative linear-ramp signal in an aberrant cancer cell.

We carry on simulations for two timespans, 114.4÷144.85min, in phase with the apoptotic time window, and 200÷1200min, respectively. For the first timespan, the results sketched in Fig. (10) show p21 upregulation almost vanishing and the remaining apoptotic species release their brakes and freely pulse toward a choral tuning at the same inflexion point at the same time location. The following apoptosis phase has no need of a second pulse and it remains permanently active.

The "tracking" properties of p21mRNA are confirmed even though it is again conceived as a negative linear-ramp signal all over a time-span of 200÷1200min (i.e., past the natural apoptotic phase in the presence of irreparable DNA damage). In fact, p21mRNA overexpression immediately occurs to intersect the inflexion point of APAF1 time rate.

This successfully occurs but two parameters come into play and change p21mRNA pathway: inversion of the p21mRNA upregulation time rate and the second pulse of APAF1. p21mRNA, like a digital CPU, exploiting to the utmost its direct "tracking memory" access, tries to follow this second pulse of APAF1 at its inflexion point for intersection. This is allowed for the second time but the third chance is denied because APAF1 reaches a steady-stable condition. According to this pulsating species dynamics, the apoptosis phase again shows two pulses and remains unchanged but with a frequency slightly lower (1.7×10^{-5}) than the natural frequency of the (unstable) apoptotic phase of a cancer cell with irreparable DNA damage.

The results sketched in the last two panels of Fig. (10) confirm the above assertions. Now, the simulations are performed using a different p21mRNA pathway (mono-cycle square-wave signal) over the same timespans (114.4÷144.85min (apoptotic timewindow) and 200÷1200min, respectively). The only difference is the p21mRNA upregulation tries to intersect the APAF1 inflexion point during its first pulse (having extremely high frequency equal to 3.61×10^{-4}) but the available remaining time window is too short for a second attempt. The apoptosis phases for both the considered timespans remain active with unchanged double-cycle pathways and natural frequencies. The simulation output for 200÷1200min (after apoptotic natural time window) is qualitatively the same of those relative to 114.4÷144.85min.

We now improved the cell master digital simulator by interlinking p21mRNA/cyclin-CDK and CDK/CDC25/wee1/SKP2/APC/CKI networks to the apoptotic mechanism. In other words, the goal of the present paper is to find and give the way for selecting cell checkpoints, sizers, timers and specific target genes dynamics both for influencing mitotic process and avoiding cancer proliferation as much as for leading the cancer cell(s) to re-enter a steady stable apoptosis phase (see details in the next section).

Unarrested Cell Cycle Depending on DNA Damage Target Genes Response for Wee1 Mutated Specie

Without loss of generality, we considered the wee1 synthesis rate reduced one order giving the mutant form, wee1(-10). To evaluate the mutant cell response to genomic
damage, we again ignored cell cycle arrest during damage repair for the same two square-wave radiation signals previously employed. For ionizing irradiation at t=0min, wee1(-10) does not affect the apoptotic target gene response for both controlled and uncontrolled cell digital biochemical mechanisms; pictorial depictions of APAF1, p53AIP1, cytoc and Apoptosome (see Fig. (15)) are the same as those obtained for the simulations described in the previous section (see Figs. (11-14)). To evaluate the global effects on cell cycle, we compare p21mRNA pulsing frequency as obtained by Qu et al. [1], over the timespan 0<t<2268.35min, to its proper oscillations. Mutated wee1 promotes initial unstable behavior of the cell division control species (two close concentration peaks of active cyclin-CDK and APC) and immediate cell division at t=75.04min triggers (see Fig. (16)); as a consequence, at the end of its cycle, the bud mass is half a “normal” cell size. Thus, we can digitally assign a key role to mutant wee1 for inducing cell sizer and checkpoint mutations.
In our model, at $t=235.7\text{ min}$, a second instability of active cyclin-CDK and APC is connected with both p21mRNA and apoptotic gene overexpressions. After a natural inertia, $t=236.26\text{ min}$, this second pathway instability of active cyclin-CDK and APC gives the “green light” to another mitosis. Almost surprisingly, despite this second unexpected division, the cell sizer will not be further affected because daughter cells will grow over a timespan 65.5\% greater than a normal sizer; then, the cell resumes its interpulse frequency (timer) and “mutant” size, the sizer being about one half a normal cell size. If p21mRNA “tracking” signaling is controlled, apoptosis is independent of the two aberrant mitotic processes (one at $t=75.04\text{ min}$ and one after p21mRNA overexpression at $t=235.7\text{ min}$) and cell death is successfully executed at $t=615.65\text{ min}$. When the ionizing irradiation signal starts at $t=1100\text{ min}$, apoptotic

Fig. (12). Output response of apoptotic species network as a consequence of DNA damage at $t=1100\text{ min}$.

Fig. (13). G_1/S\rightarrow G_2/M transition species and cell mass evolution (growth not halted and DNA damage starting at $t=0\text{ min}$).
network responses are the same (and only shifted) as those obtained for \( t=0 \text{min} \) (see Fig. (17)). Cell growth factor dynamics, in terms of sizer and timer variations, persist in such a mutant wee1 presence and are qualitatively the same as those displayed in Fig. (16), (see Fig. (18)). Natural p21mRNA “tracking” signal triggering and the extent of the genomic damage (if not completely repaired) push the overall cell system towards tumorigenesis; meanwhile, if p21mRNA upregulation signaling is governed by an optimum control law (dashed line in Fig. (18)) proliferation is halted whatever the cell divisions. Similarly, when the ionizing irradiation signal is emitted at \( t=1100 \text{min} \) and the third mitotic process is overcome, programmed cell death is executed at \( t=1705.15 \text{min} \).

**DISCUSSION**

To check the reliability of the employed multi-nested digital platform vs. *in vitro* evidence, we also take into account the analysis of the effects of PML-RAR on p21 in p53 for leukaemia stem cells showed by Viale *et al.* [55] in which p21 upregulation by PML-RAR is p53-independent. Once the digital platform was tuned to replicate this network
In agreement with but differently from Viale et al., we deduce and confirm that p21mRNA upregulation is p53-independent over the initial frame of the global timespan. The discrepancy between our results and those of these authors is superficial not only computationally speaking. In fact, the overexpression of p21mRNA digitally triggers within a very small interval and its intensity (and gradient), more similar to a saturation signal, is quite different from those of the other gene expressions. This behavior, typically digital, implies two effects: first, p21mRNA upregulation becomes almost invisible when one has to evaluate its effects in back-reactions and experimental tools might fail in detecting it unless they are provided with suitable digital plug-ins; secondly, if one admits as negligible the p53-dependence of p21mRNA overexpression, this could become supercritical for the apoptotic network. Roughly speaking, the involvement of p21mRNA in apoptosis avoidance is unveiled taking into account APAF1 as a marker.

In this way, peculiar features of the proposed model are underlined if one considers that these digital cell layers are now capable of detecting and controlling molecule signaling pathways during and (mainly) after the division process if cell growth is not arrested (see Cell Mass panels in Figs. 16 and 17).
In this case, the cell digital control platform is independent of DNA damage triggering and switches itself from single cell to multi-cellular configuration, i.e., it starts to sequence and control cell divisions and acts successively on the cell cycle dynamics parameters of both mother and daughters. In other words, if a damaged genome is detected and p53/Mdm2 defects, the controlled cell defence resources alarm checkpoints, timers and sizers to avoid proliferation and/or execute programmed cell death. This set of by-products is digitally highlighted by the peculiar and different double-pulsing outfits of p21mRNA (chorally with active-CDK complex, cell mass, wee1 and APC) depending both on apoptotic gene instabilities and cell cycle time windows. As regards the apoptotic species network only, it switches on the alert at an exact time location, i.e., when the target gene gradients---even though still growing---start to invert their time rates. This universal convergence criterion leads to the gene gradients for decrypting the apoptosis code. The proposed cell digital simulator model demonstrates how the whole cell apoptosis network rigorously falls into line with this principle and suggests the mechanism for apoptosis stimulation and stabilization.

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